



# Reserving with Simulation

IFoA Asia Conference 2016

NMG Consulting

3 March 2016

# Contents

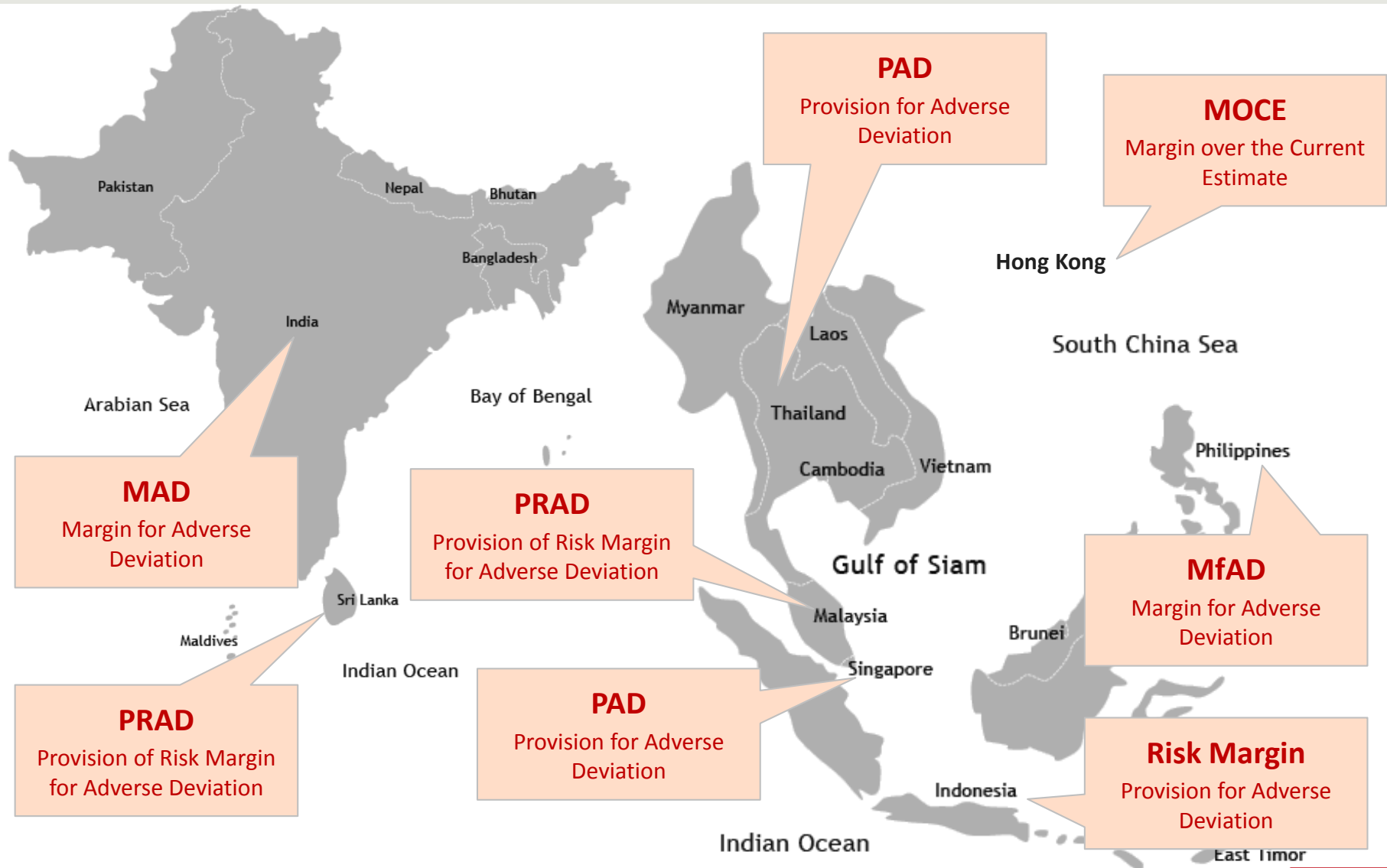
**Section 1: What are risk margins?**

**Section 2: Claim Liability risk margin**

**Section 3: Premium Liability risk margin**

**Section 4: Conclusions**

# Risk margins



# Why do we need them?

## Market Value Accounting



75<sup>th</sup> percentile is the common ground in determining the risk margin / margin to transact something at an arm's length

## Consistency in Solvency

**RISK BASED  
CAPITAL**

Many countries in the region are using the RBC approach for determining the capital requirements

## Properties



Increased uncertainty in the current estimate of liabilities and its trends



**Higher risk margins**

# The uncertainties

## Claim Liability

- Claims experience in the past
- Earned exposure

## Premium Liability

- Prospective claims experience
- Unearned exposure



Variability in  
future trends



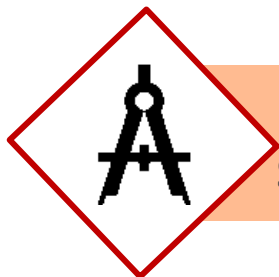
Data error



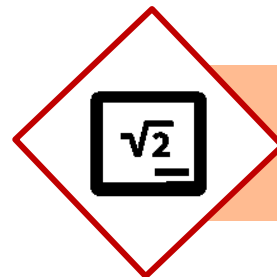
Process error



Reinsurance risk



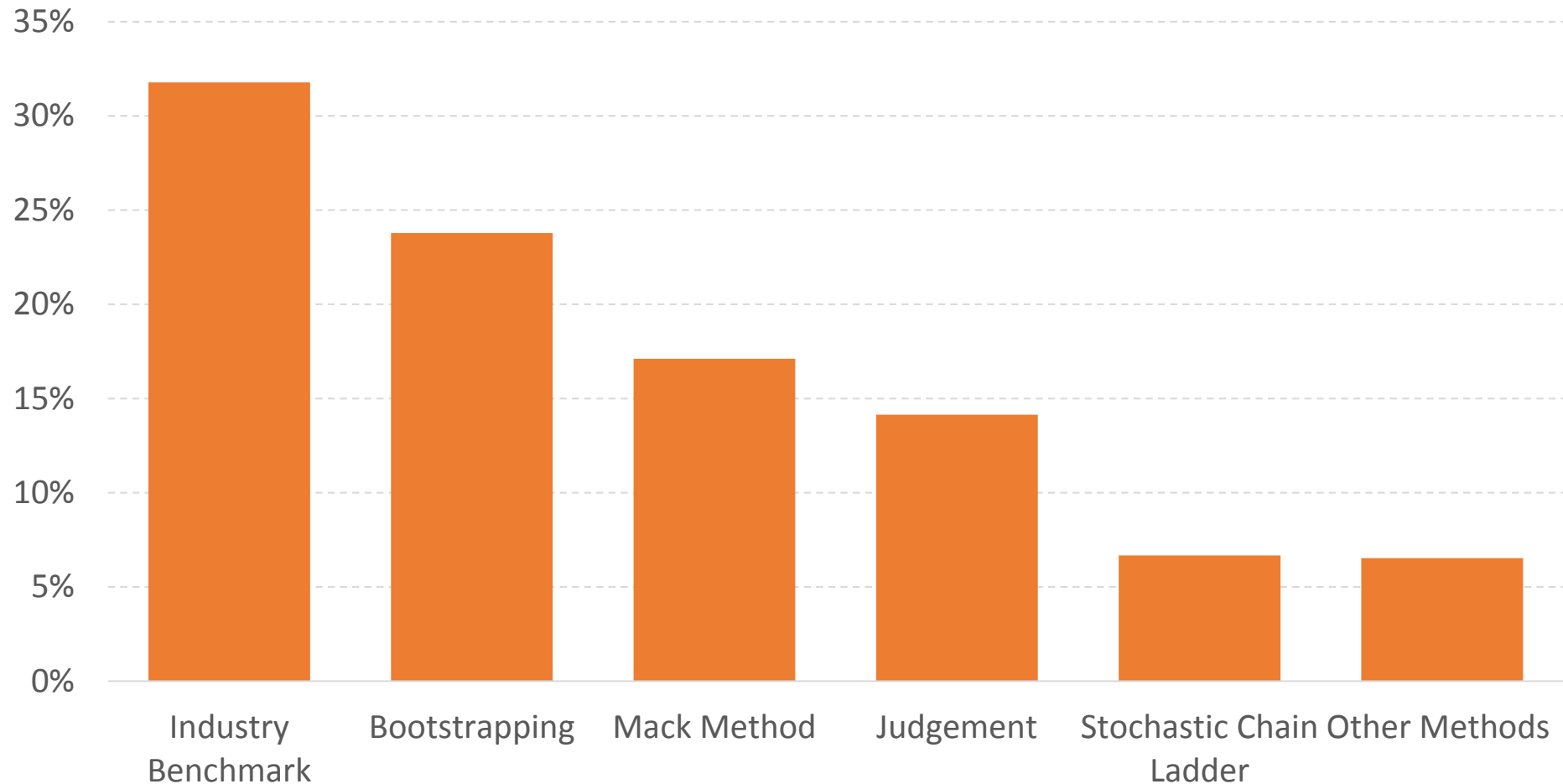
Model  
Specification error



Parameter error

## How are they determined? – Singapore

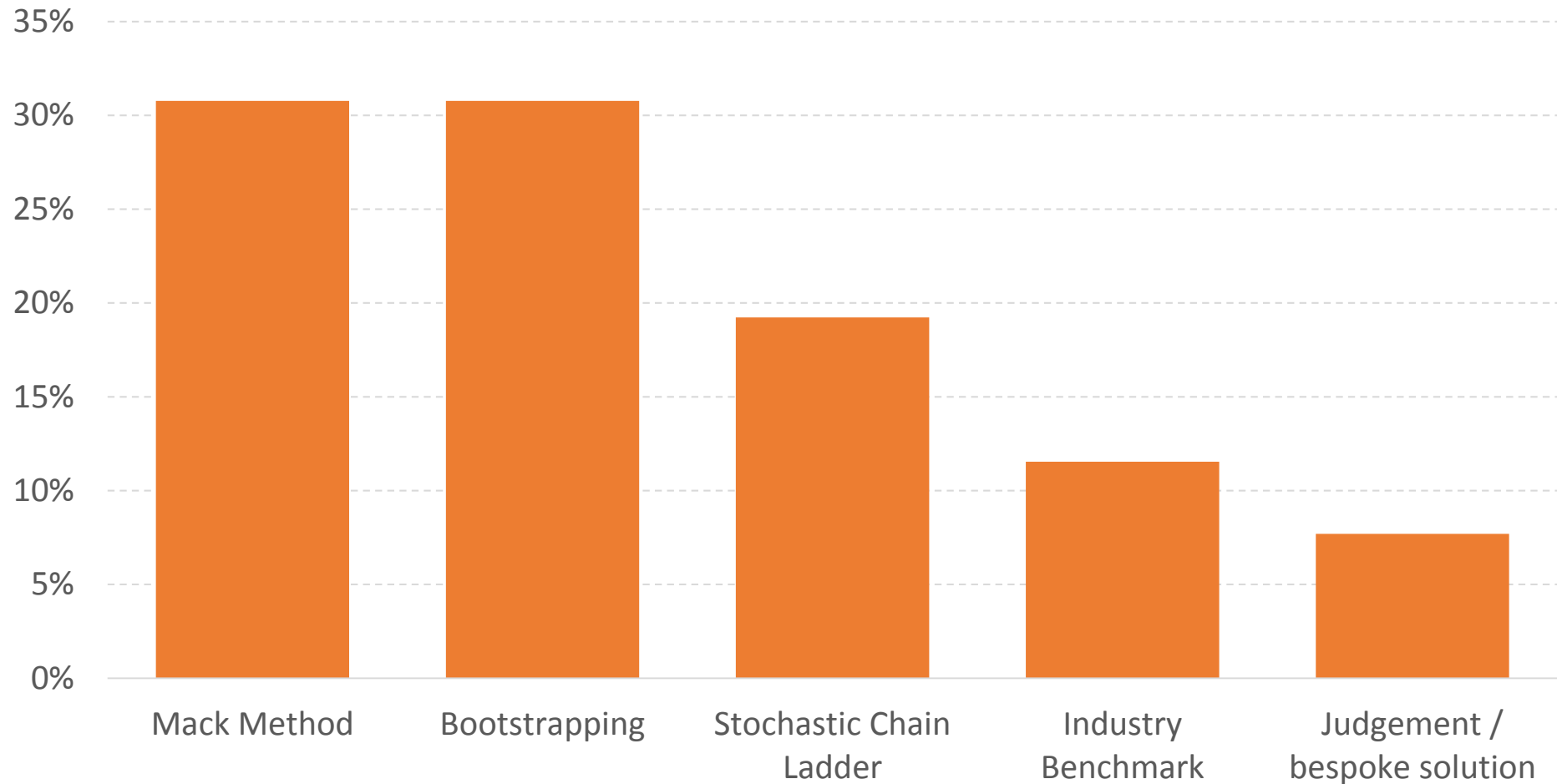
### Methods used - Claim Liability risk margins



*\*Based on MAS 2013 stats*

## How are they determined? – Malaysia

### Methods used - Claim Liability risk margins



# Claim Liability risk margin – the methods

## Judgement

- Based on the actuary's past experience or general reasoning
- + The actuary may take into account additional factors not captured within the data
- Fairly subjective method and hence a risky process

## Industry Benchmark

- Adoption of risk margins according to Industry Benchmark by line of business
- + Useful for **companies which lack historical claims data**
- **May not be reflective of the Company's true variability** of the liability estimates

## Mack Method

- Measures the **Mean Square Error** of the overall claims reserve
- Based on chain-ladder assumptions
- + Usually provide **stable results**, measuring parameter, process and total risk
- Does not explicitly measure **tail variability**

## Bootstrapping Method

- A resampling method used to consistently estimate the variability of parameters
- + **No assumptions about the underlying distribution** is required
- + Powerful and simple, using only a single data set
- Variability limited to that in the underlying historical data



# Claim Liability risk margin – the methods

## Judgement

- Based on the actuary's past experience or general reasoning
- + The actuary may take into account additional factors not captured within the data
- Fairly subjective method and hence inconsistent process

## Industry Benchmarks

line of business

## Market

and total risk

## Bootstrapping Method

- A resampling method used to construct estimate the variability of parameters
- + **No assumption about the underlying distribution** is required
- + Powerful and simple, using only a single data set
- Variability limited to that in the underlying historical data

**The analysis performed in deriving the Central Estimate of the liabilities is disregarded!**

# Industry Benchmark

**Tillinghast-Towers  
Perrin Risk Margin  
Study [2001]**

**APRA Risk Margin  
analysis: Collings and  
White – Trowbridge  
Consulting [2001]**

**Simple average of risk  
margins from other  
insurance companies**



- Studies conducted are based on different:
  - regulatory environment
  - product features / tariff
  - economic environment
  - distribution channel



- Few reasons to justify why this is accurate and should be implemented in the local market

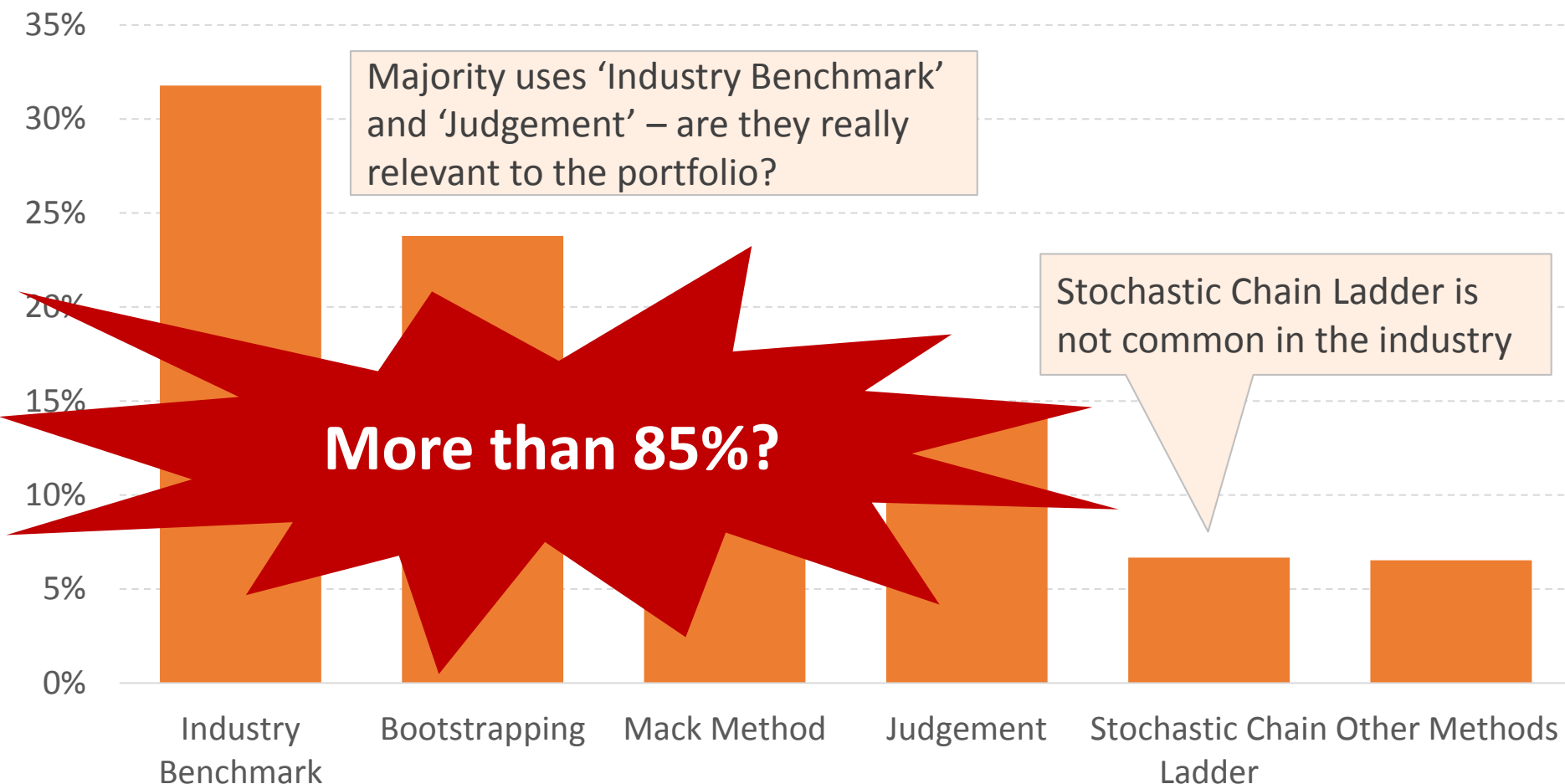


- Every company operates differently – benchmark risk margins may not reflect the true volatility of the liabilities

***All companies are NOT the same***

# How are they determined? – Singapore

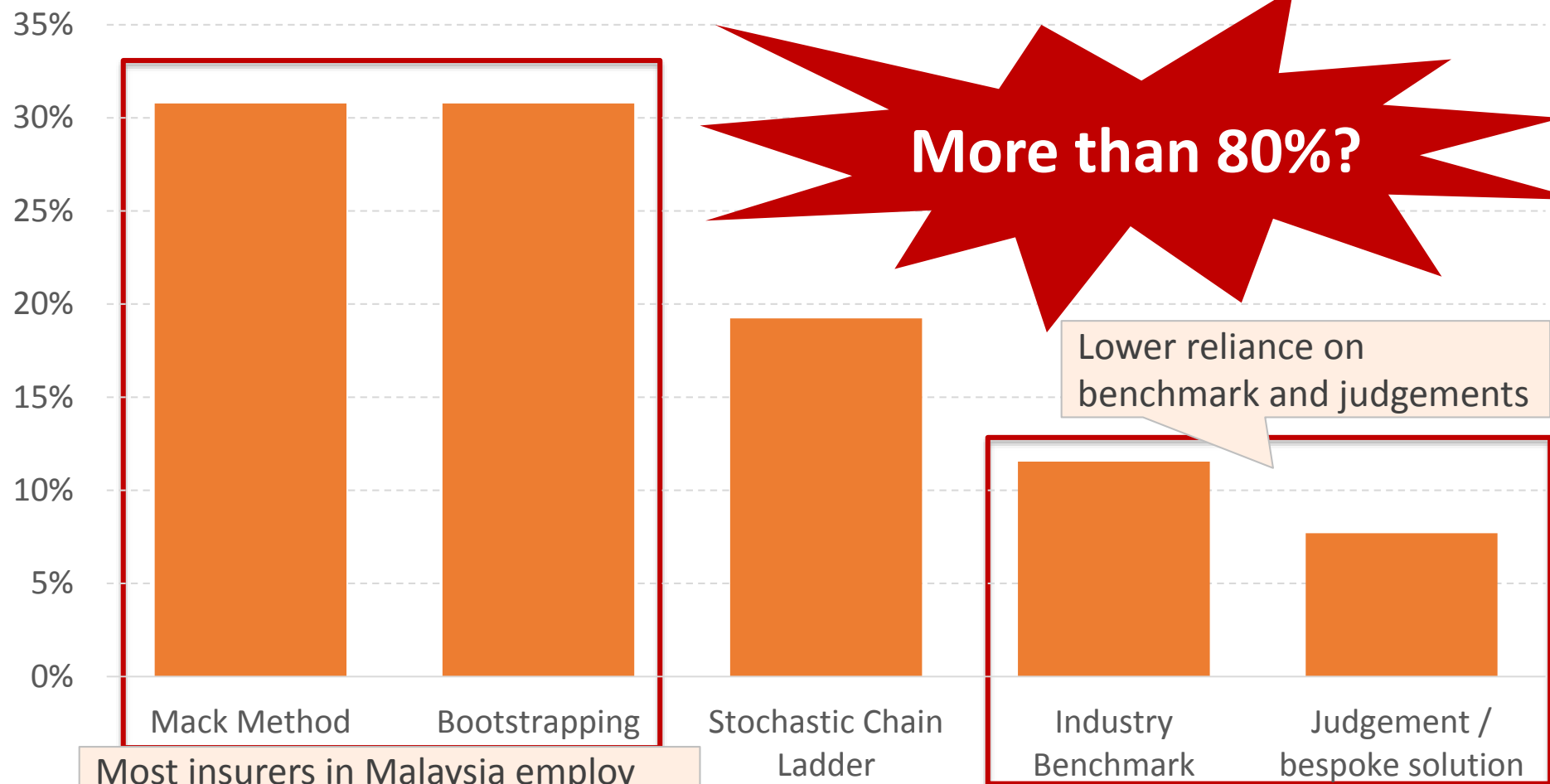
## Methods used - Claim Liability risk margins



\*Based on MAS 2013 stats

# How are they determined? – Malaysia

## Methods used - Claim Liability risk margins



# Claim Liability risk margin – the methods

## Stochastic Chain Ladder Method

- Development Factors are assumed to be **Lognormal** distributed
- Flexible, can incorporate the development period effect explicitly
- + **Correlations across periods** can be accommodated
- Requires statistical software for faster simulation

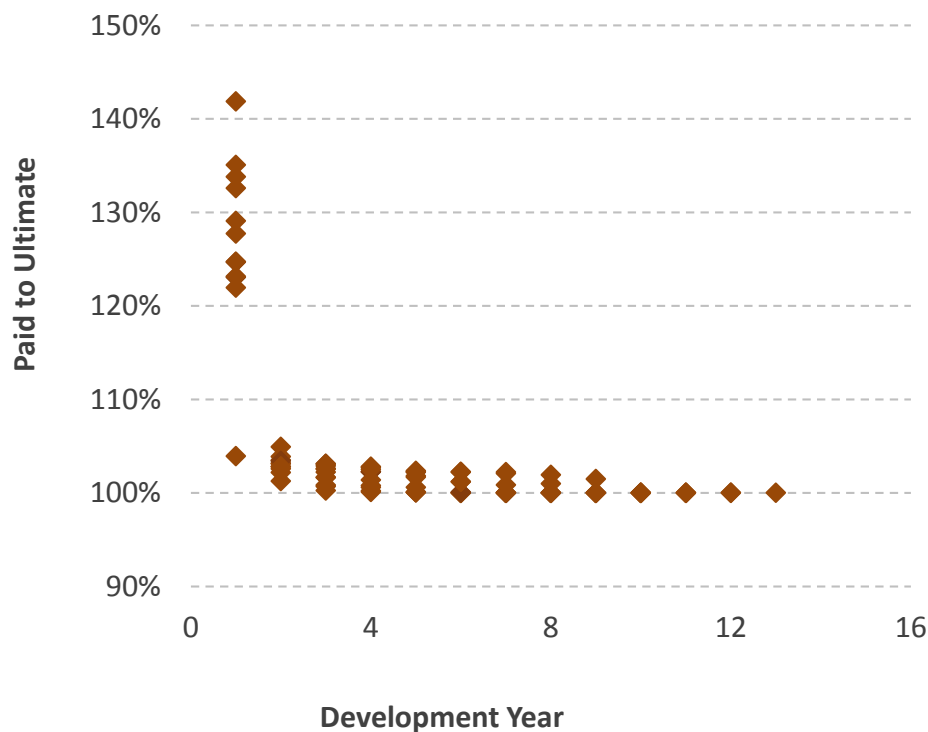


# Stochastic Chain Ladder Method

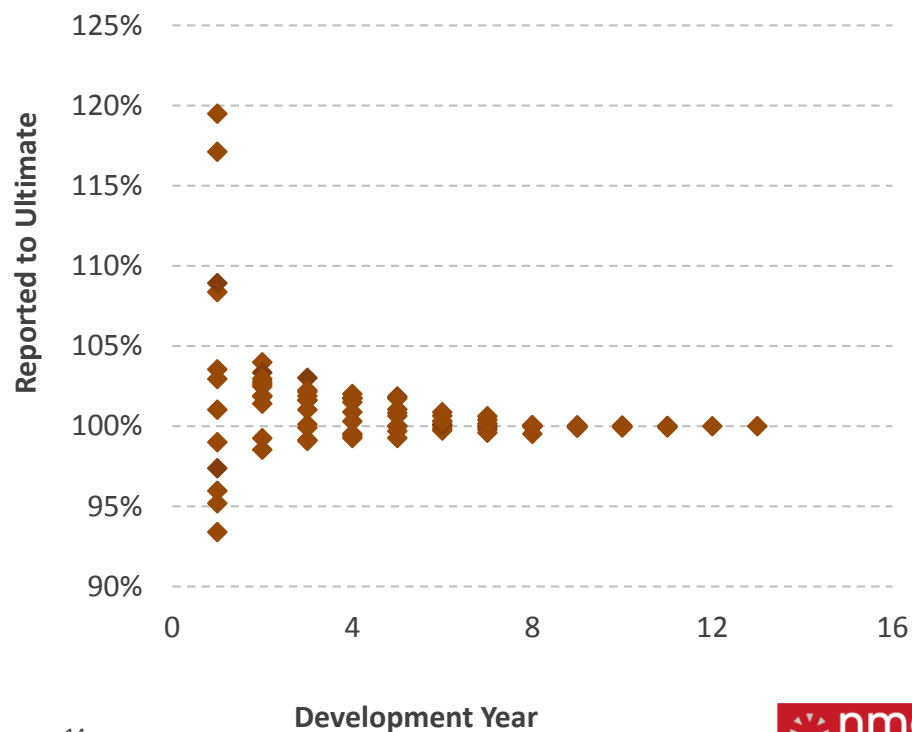
## Stochastic Chain Ladder Method – Motor class from a regional insurer

- 1 Determine the implied paid / reported cumulative LDFs for each Accident Year and for each development period**

Paid Analysis



Reported Analysis



# Stochastic Chain Ladder Method

## Stochastic Chain Ladder Method – Motor class from a regional insurer

### 2 Determine the parameters for simulating the cumulative LDFs

Paid Example	Accident Year	2011	2012	2013	2014	2015
	Development Factor (Year 1 to Ultimate)	109%	117%	119%	101%	104%

(a)	Average (2011 to 2015)	=	110%
(b)	Standard Deviation (2011 to 2015)	=	8%
(c)=(b)/(a)	Coefficient of Variation	=	7%

# Stochastic Chain Ladder Method

## Stochastic Chain Ladder Method – Motor class from a regional insurer

### 3 Simulate the cumulative LDFs and derive the revised Ultimate Loss

<b>Paid Example</b>	<b>Accident Year</b>	<b>2011</b>	<b>2012</b>	<b>2013</b>	<b>2014</b>	<b>2015</b>
	Simulated Development Factor (Year 1 to Ultimate)	102%	102%	102%	103%	109%
	Paid to Date	199	369	557	617	680
	Ultimate Loss	202	374	567	635	742

- Assume a Lognormal distribution for the cumulative LDFs
- Sum the Ultimate Loss across Accident Years and determine the overall 75<sup>th</sup> percentile value
- Subtract the Central Estimate of the Ultimate Loss from this value to determine the risk margin



# Stochastic Chain Ladder Method

## Existing methodology:



Lognormal distribution reflects the positively skewed nature of GI claims



Simulations based on the calculated Central Estimate



Outliers removed from original data



Allows judgement for past experience

## Issues:



Model error



Reality is one simulation only – results will differ if the sample is changed



Need an objective approach to remove outliers



Results are subject to individual judgements – need to automate to run simulations

# Stochastic Chain Ladder Method

## Enhancements introduced:



Automation of outlier removal

- based on the number of points and mean & standard deviation of the lognormal distribution



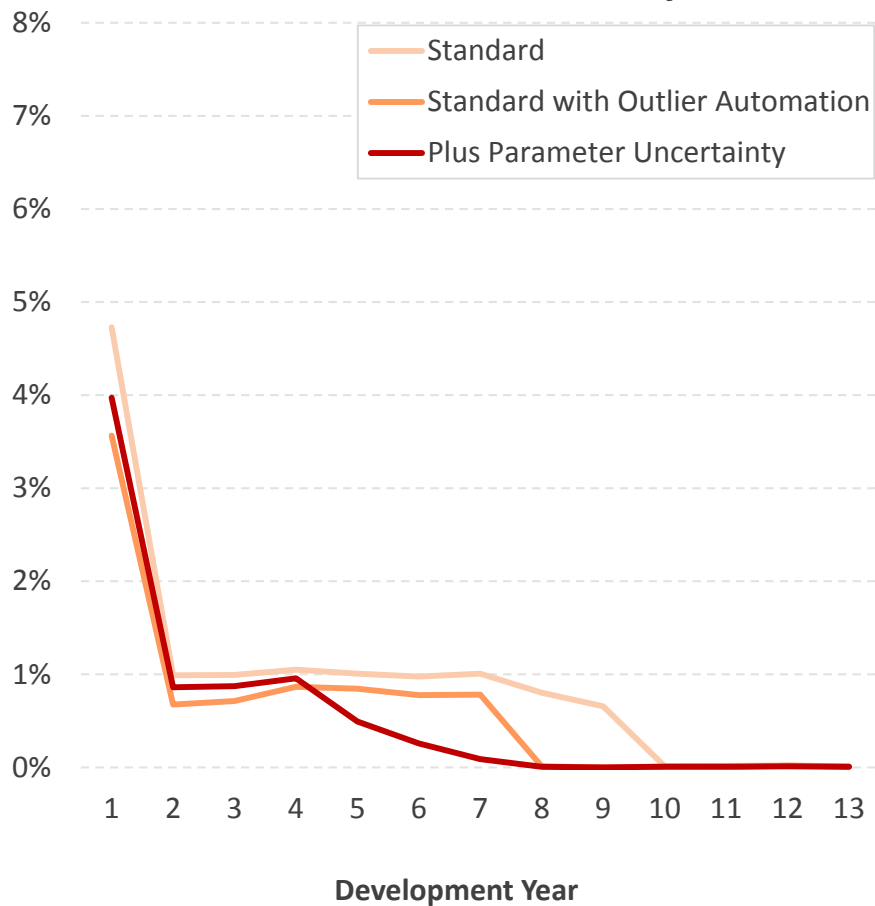
Parameter uncertainty

- re-simulate the claim triangles

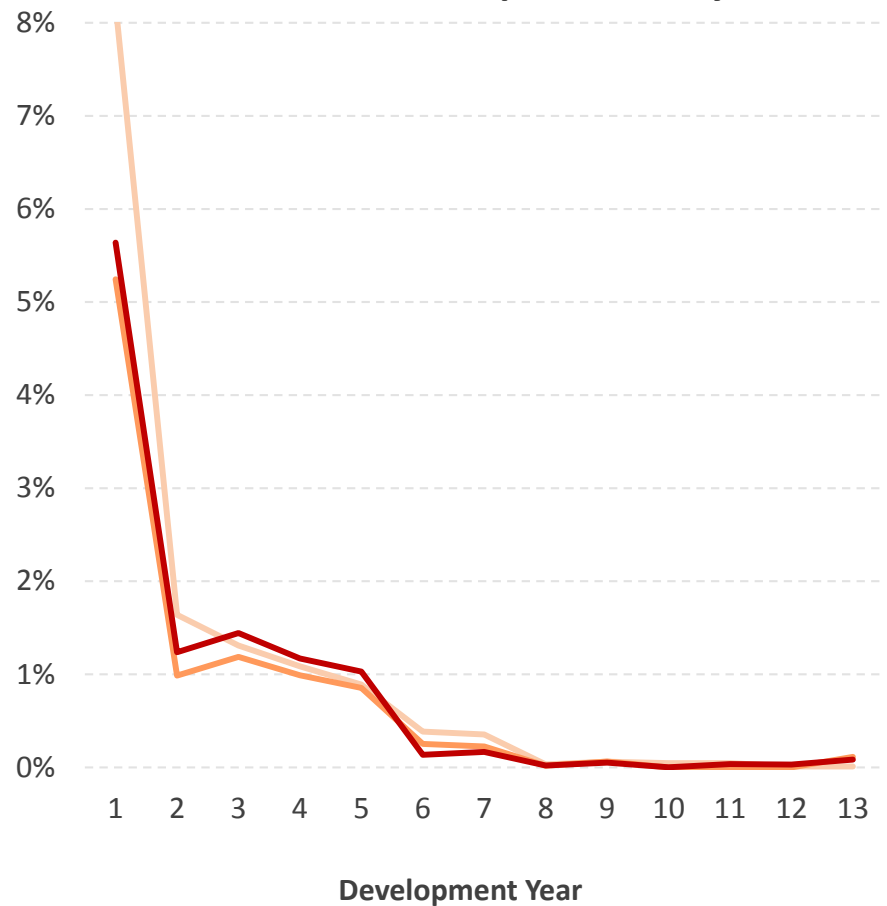
# Enhanced Stochastic Chain Ladder Method

## Stochastic Chain Ladder Method – Motor class from a regional insurer

### CoV Movement – Paid Analysis



### CoV Movement – Reported Analysis



# Enhanced Stochastic Chain Ladder Method

## Stochastic Chain Ladder Method – Motor class from a regional insurer

### Comparison of the risk margin:

	Industry Benchmark		Stochastic Chain Ladder	
	*APRA	<sup>^</sup> Tillinghast-Towers Perrin	Standard with Outlier Automation	Plus Parameter Uncertainty
75% Risk Margin	13.1%	8.0%	16.3%	<b>22.0%</b>

\* APRA General Insurance Risk Margins Industry Review report as at 30 September 2013, published 17 February 2015

<sup>^</sup> Tillinghast-Towers Perrin Risk Margin Study – Research and Data Analysis Relevant to the Development of Standards and Guidelines on Liability Valuation for General Insurance, published 20 November 2001

# Summary

## Industry Benchmark & Judgement

~**50%** of the insurers  
in Singapore

~**20%** of the insurers  
in Malaysia

**Relevance?**

## Mack Method & Bootstrapping

~**40%** of the insurers  
in Singapore

~**60%** of the insurers  
in Malaysia

**No relationship to the  
Central Estimate!**

## Summary

**Industry Best  
& Justification**

**Link Method &  
trapping**

**Time for a  
change?**

~**50%** of the insurers in Singapore

~**20%** of the insurers in Malaysia

**Relevance: Relationship to the  
Central Estimate!**

## Common myth

### Question 15:

In terms of percentage, the volatility of the URR should be greater than the volatility of the Claim Liability. We observe in terms of Net liabilities for all lines excluding Marine, the loadings for CL liability are greater than Premium Liability. If we were to look into volatility by each accident quarter the recent quarter would be expected to be most volatile, given we assume the selected payment/reporting patterns will follow.

### Question 2:

What is the rationale for allowing a lower PRAD in premium liabilities compared to the PRAD in OSC for these classes given that there is typically greater uncertainty in estimating premium liabilities?

5) Could you share with us how the PRAD loading for premium liability are selected after comparing with results from previous analyses, including APRA study?

## Common myth

### Quotes from APRA Risk Margin Analysis 2001

“It is generally recognised that the volatility of the premium liabilities of a class will be **greater than that for outstanding claims.**”

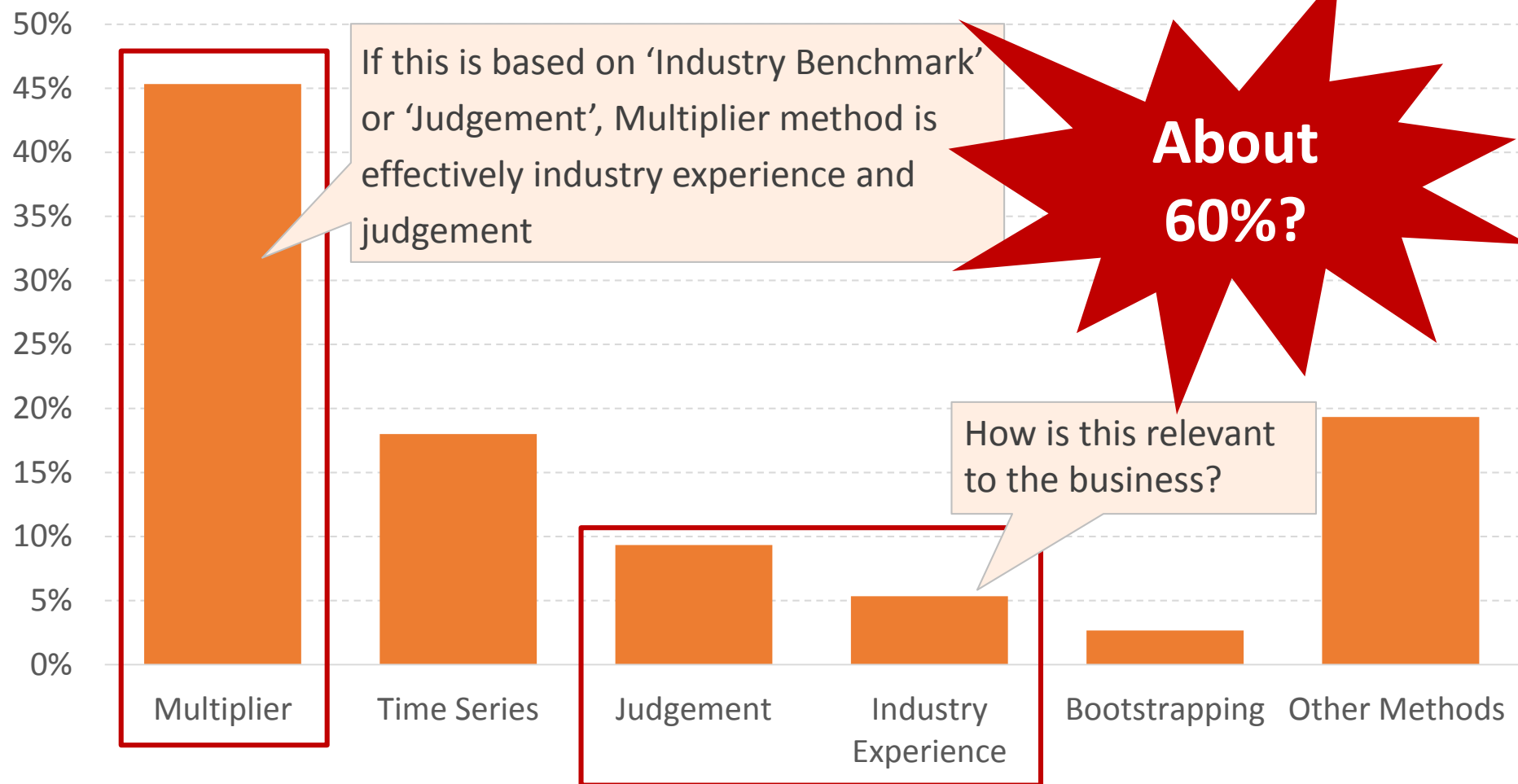
“This is because the **exposure period** for these liabilities has not yet occurred and events such as **future catastrophes** need to be allowed for.”

“Premium liabilities should contain a slightly **greater degree of variability** to that of the most recent accident year”



# How are they determined? – Singapore

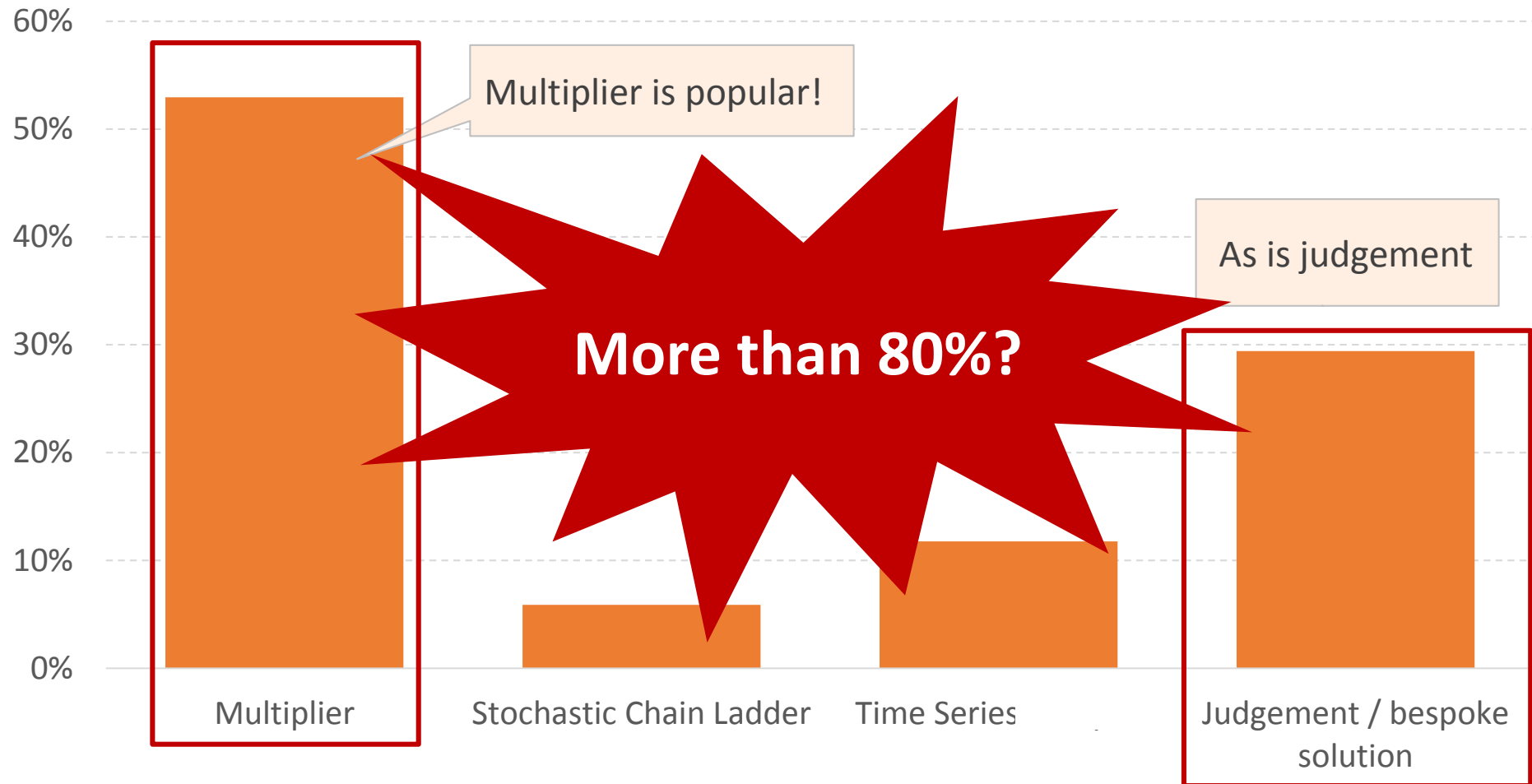
## Methods used - Premium Liability risk margins



\*Based on MAS 2013 stats

## How are they determined? – Malaysia

### Methods used - Premium Liability risk margins



# Debunking the myth: Part 1

## APRA has moved on from 2001!

Ratio of PL to OCL risk margins

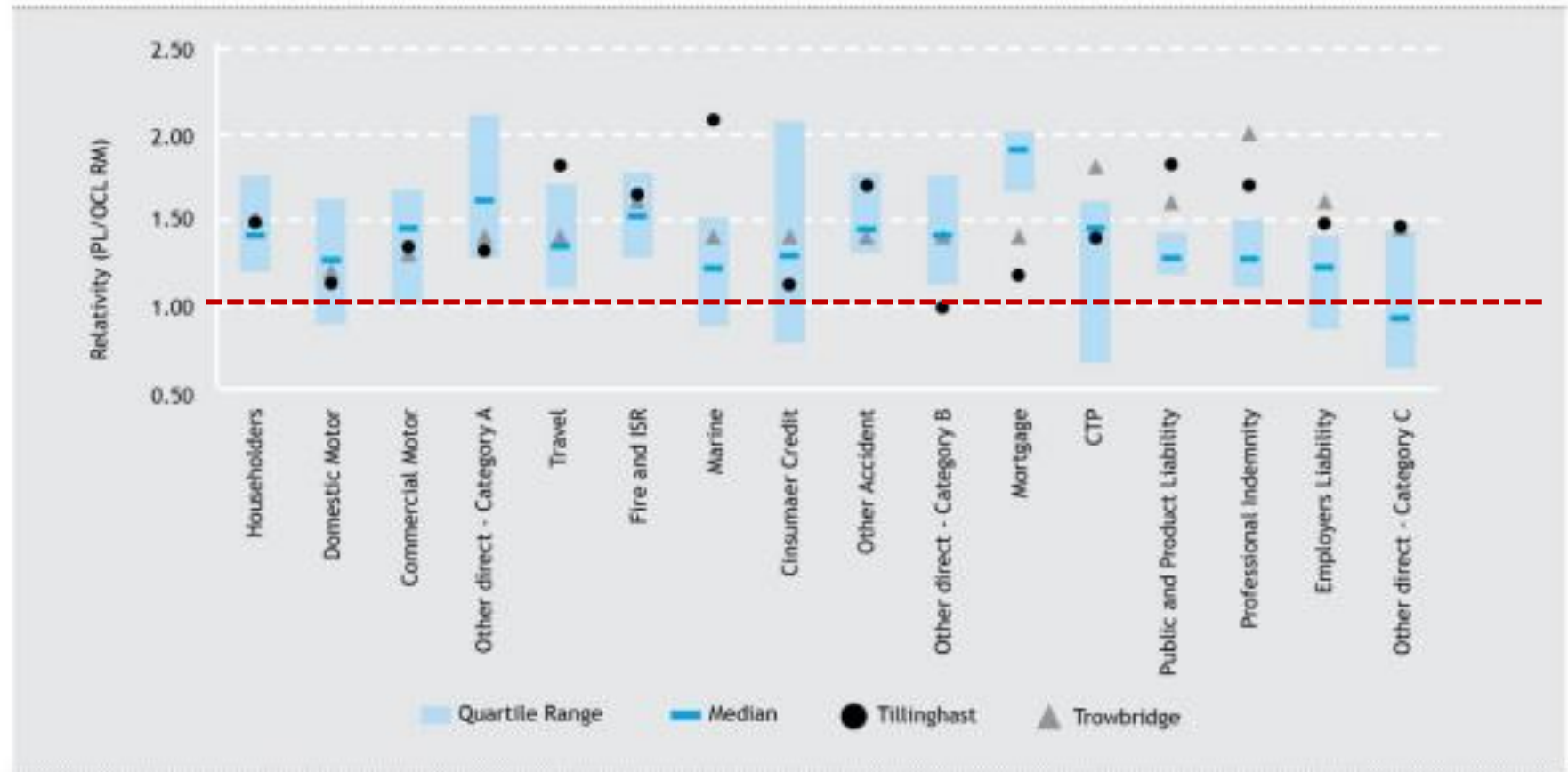
Direct Classes	PL Scale Up Factor Quartiles			Tillinghast	Trowbridge
	1 <sup>st</sup>	2 <sup>nd</sup>	3 <sup>rd</sup>		
Householders	1.19	1.40	1.75	1.48	1.50
Domestic Motor	0.88	1.26	1.61	1.13	1.20
Commercial Motor	1.01	1.45	1.67	1.33	1.30
Other direct - category A	1.27	1.61	2.10	1.32	1.40
Travel	1.10	1.34	1.70	1.81	1.40
Fire and ISR	1.27	1.52	1.76	1.64	1.60
Marine	0.88	1.22	1.51	2.07	1.40
Consumer Credit	0.78	1.29	2.06	1.12	1.40
Other Accident	1.30	1.44	1.77	1.69	1.40
Other direct - category B	1.12	1.41	1.75	0.99	1.40
Mortgage	1.66	1.90	2.00	1.17	1.40
CTP	0.67	1.44	1.60	1.40	1.80
Public and Product Liability	1.18	1.27	1.42	1.81	1.60
Professional Indemnity	1.10	1.26	1.49	1.69	2.00
Employers Liability	0.86	1.22	1.40	1.47	1.60
Other direct - category C	0.64	0.93	1.43	1.45	1.45

\*APRA General Insurance Risk Margins – Industry Review report as at 30 September 2013, issued 17 February 2015

# Debunking the myth: Part 1

## APRA has moved on from 2001!

Figure 6: PL Scale up Factors by Class of Business



## Debunking the myth: Part 2

### **Suggested CV Multipliers from APRA Risk Margin Analysis 2001**

<b>Class of Business</b>	<b>CV Multiplier Range</b>
Long Tail	1.6 – 2.0
Short Tail	1.2 – 1.6

# Debunking the myth: Part 2

Long-Tail	Claim Liability	Premium Liability
Premium	1,000	1,000
Expected ULR	80%	80%
Paid	100	0
Outstanding	700	800
CV Multiplier		1.8
Risk Margin (75%)	10%	18%
75% ULR	87%	94%
ULR Increase	8.75%	18.00%

## Debunking the myth: Part 2

Short-Tail	Claim Liability	Premium Liability
Premium	1,000	1,000
Expected ULR	80%	80%
Paid	600	0
Outstanding	200	800
CV Multiplier		1.4
Risk Margin (75%)	10%	14%
75% ULR	82%	91%
ULR Increase	2.50%	14.00%

**5.60**

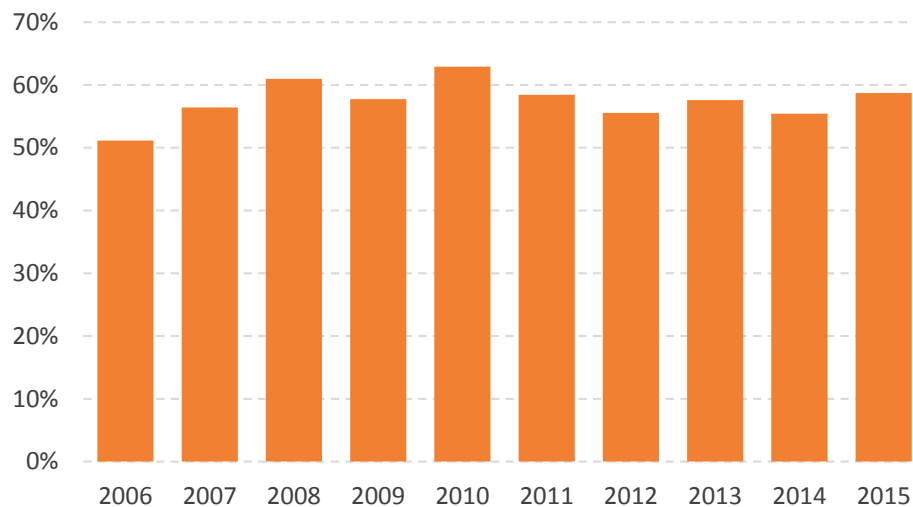
# Debunking the myth: Part 3

Year 1

Paid in Year 1 (80%)

Claim Liability  
(20%)

PLR at Year 1



Average

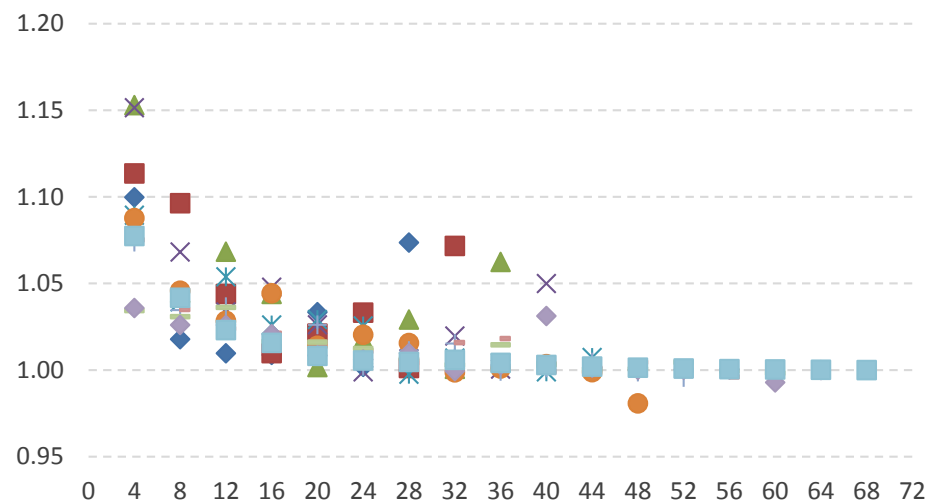
57.5%

St Dev

3.1%

- 75% load based on a Lognormal distribution = 8%

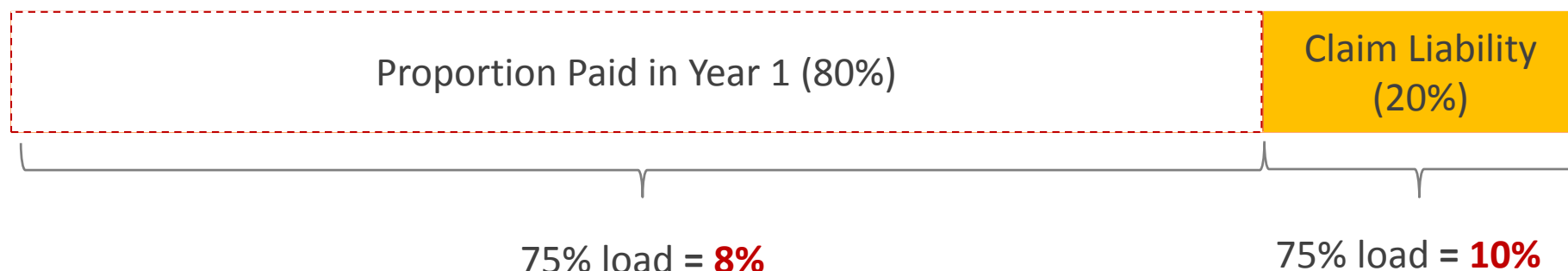
Reported Analysis



- 75% load based on a Stochastic Chain Ladder = 10%



## Debunking the myth: Part 3



### Results

Volatility of Premium Liability,  
at 75% confidence level

$$= 80\% * 8\% + 20\% * 10\%$$

$$= \mathbf{8.4\%}$$

Less than the Claim  
Liability risk margin of **10%**

### Comments

- Volatility of URR and volatility of Claim Liability are based on very different processes
- URR includes a large body of claims that are reported and paid in the first development year that are relatively stable, and so do not get included in the claim liability figures

## Common myth

### Quotes from APRA Risk Margin Analysis 2001

“It is generally recognised that the volatility of the premium liabilities of a class will be greater than that for outstanding claims.”

“This is because the exposure period for these liabilities has not occurred and events such as future catastrophes need to be allowed for.”

“Premium liabilities should contain a slightly greater degree of variability to that of the most recent accident year”

# Time series method

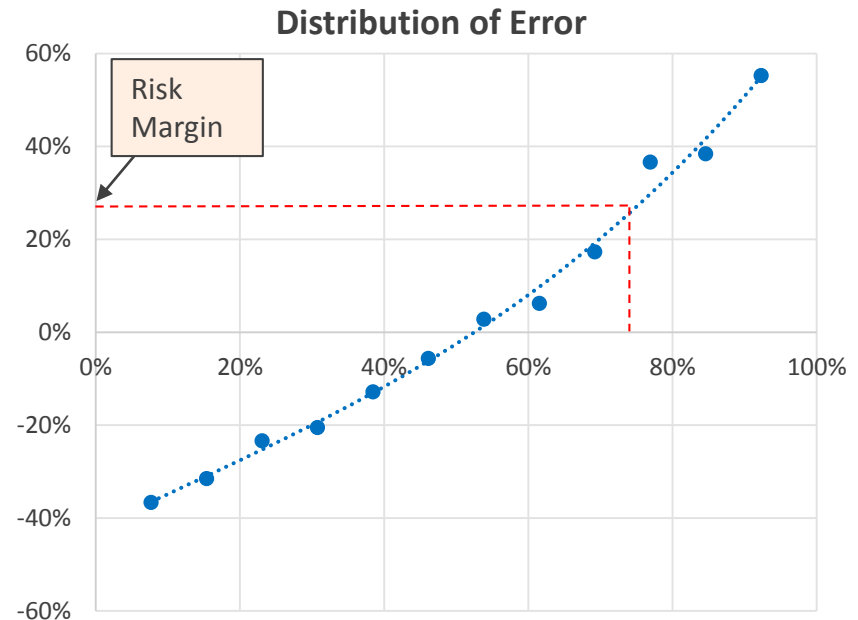
- Comparison of the historical projections of URR with the latest estimates
- Determines distribution of the standard errors and select the appropriate confidence level

## Pros

- Utilises data of many prior years
- Able to determine the most appropriate method to project URR for different classes
- **Does not rely on any assumptions on distribution** of claims

## Cons

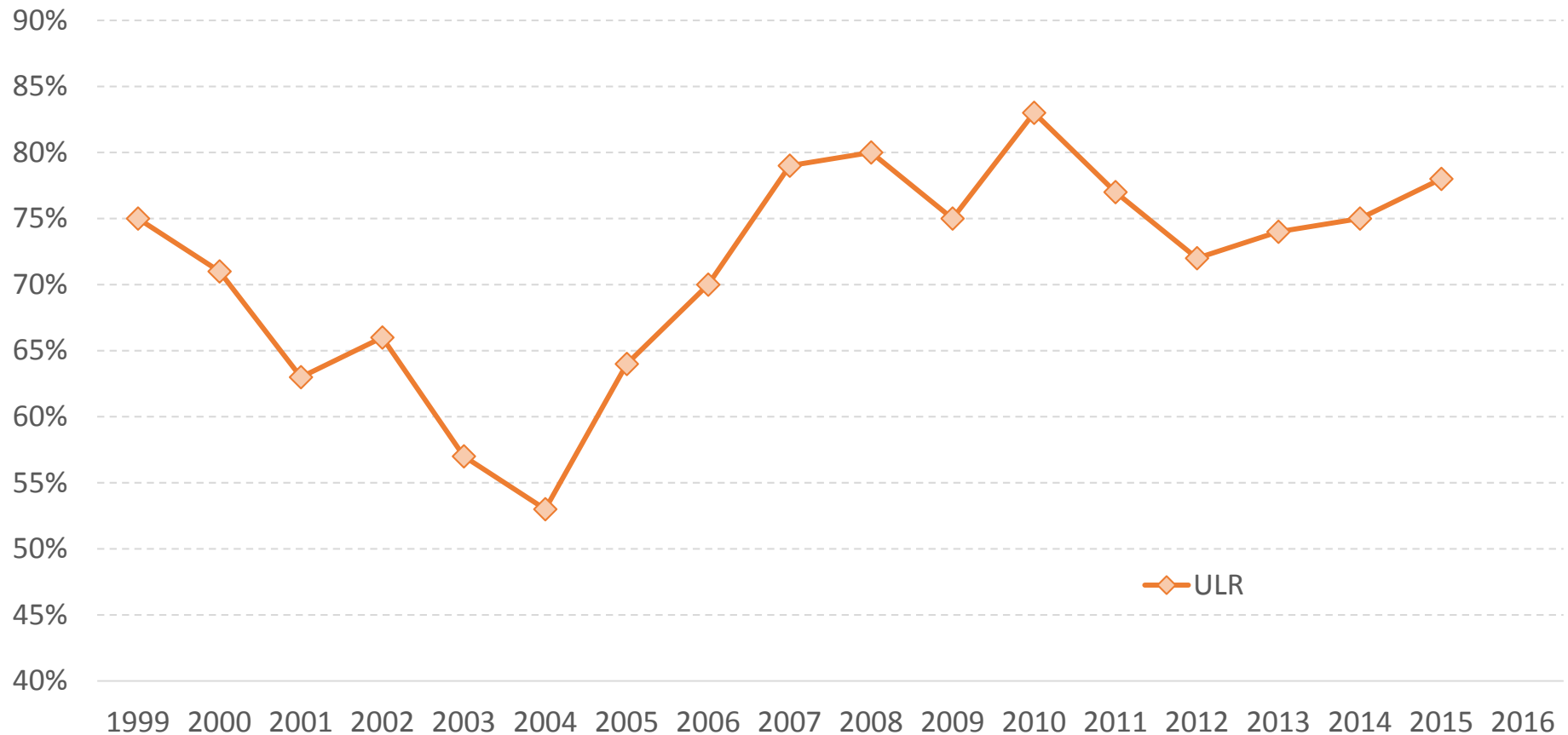
- Complex and difficult to understand
- **Outliers** can distort results



# Time series – how does it work?

**Step 1:** Obtain the selected ULR from Claim Liability analysis

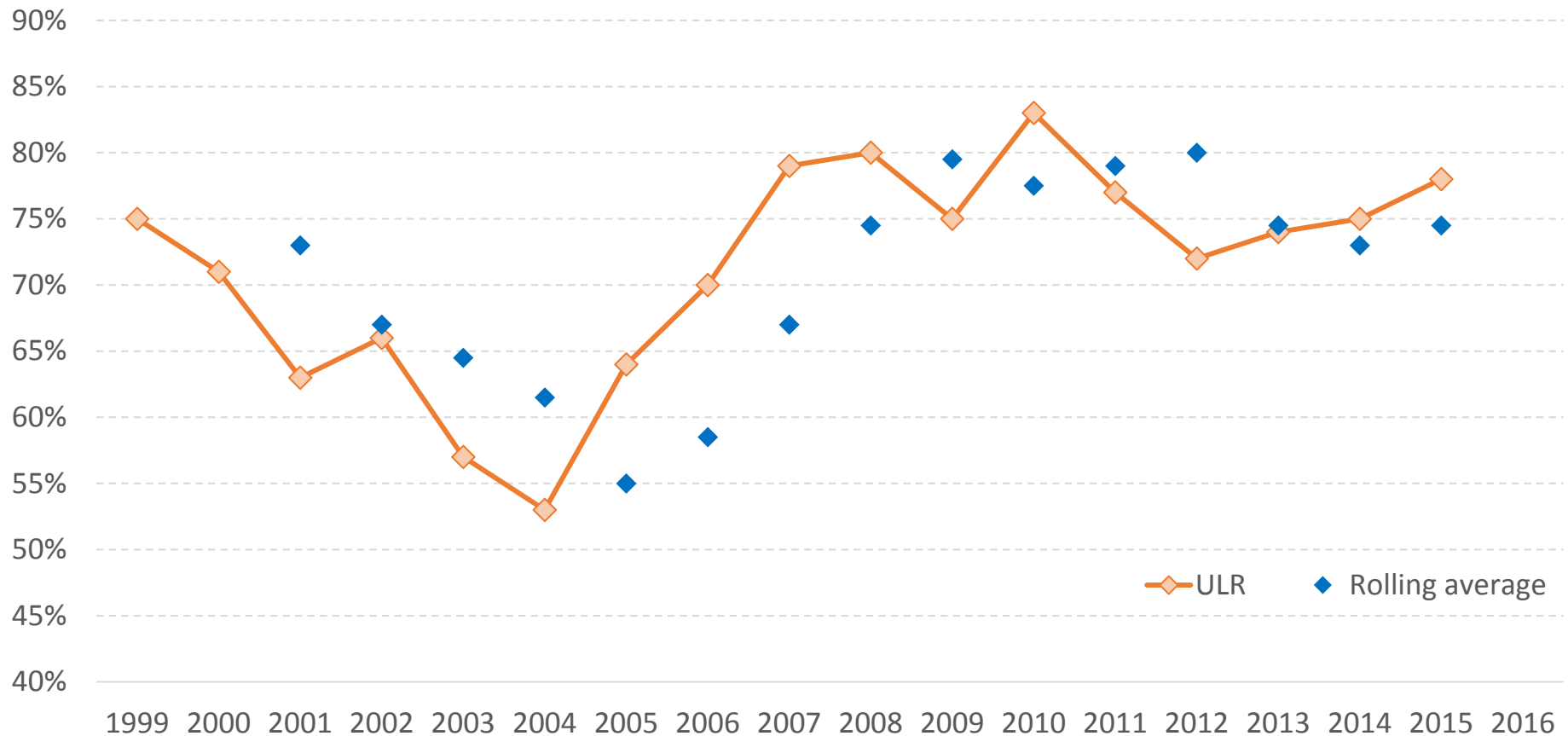
## Motor class from a regional insurer



# Time series – how does it work?

## Step 2: Calculate the two years rolling average ULR

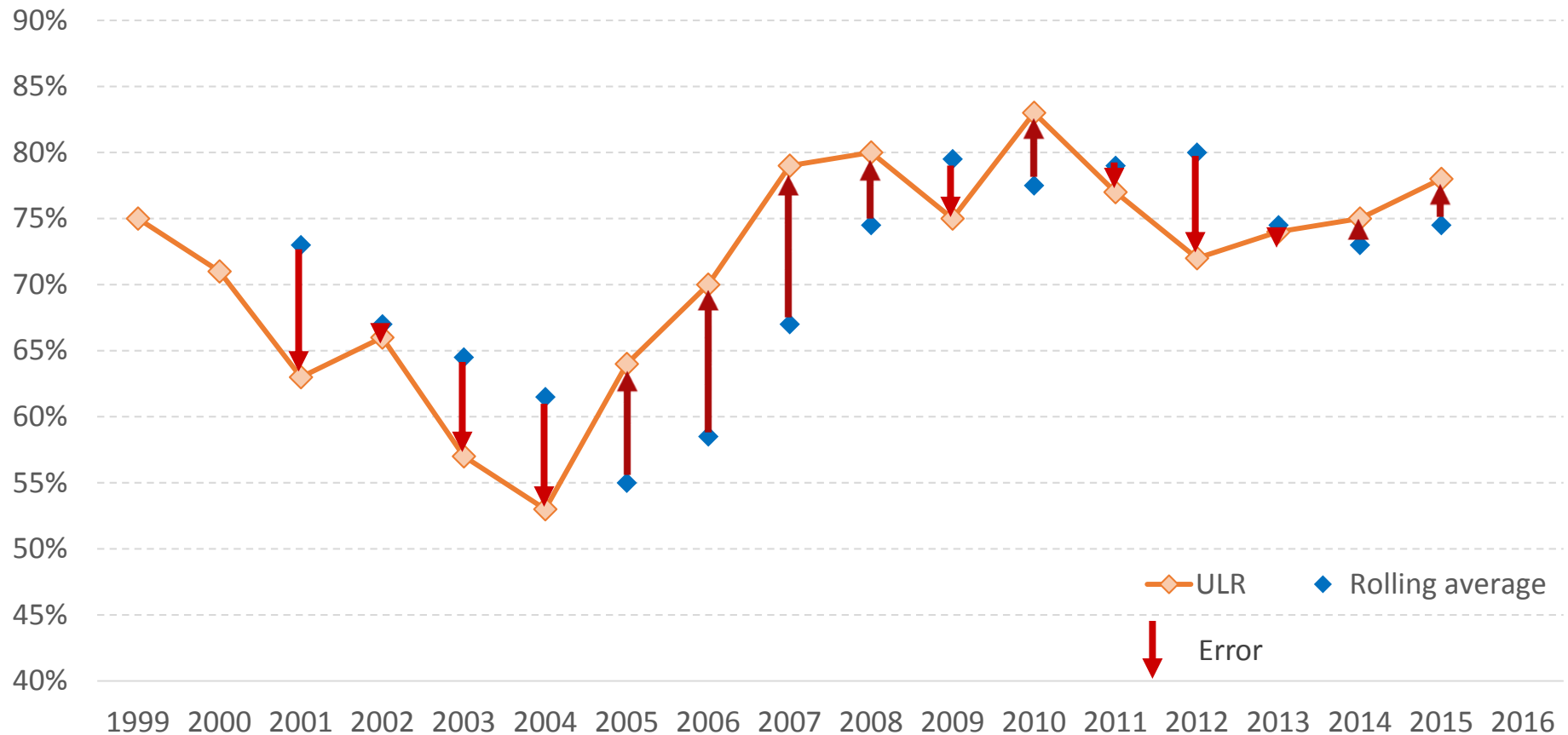
### Motor class from a regional insurer



# Time series – how does it work?

**Step 3:** Calculate the error between the selected ULR and rolling average ULR

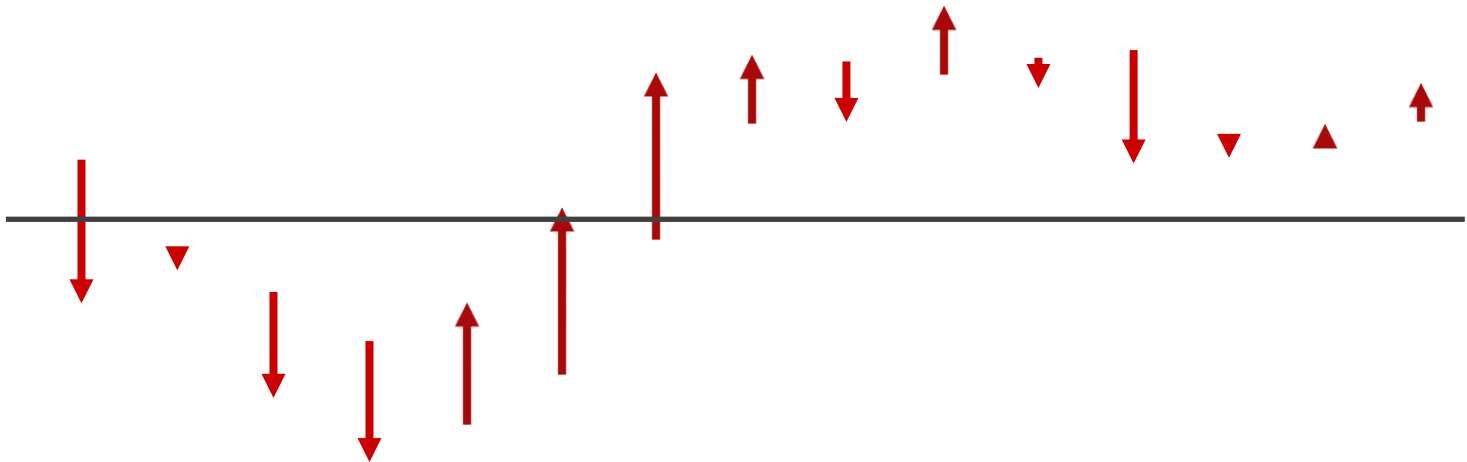
## Motor class from a regional insurer



# Time series – how does it work?

## Step 4: Rank the errors and fit a trendline

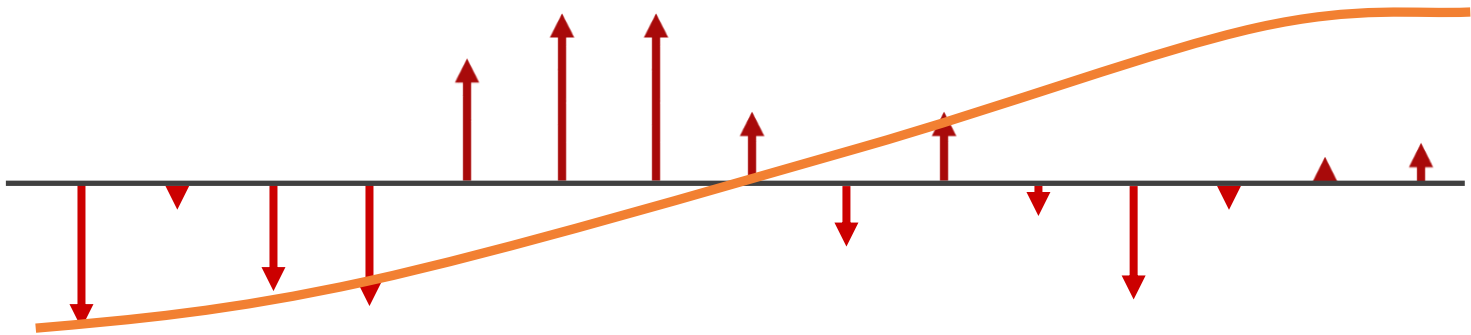
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# Time series – how does it work?

## Step 4: Rank the errors and fit a trendline

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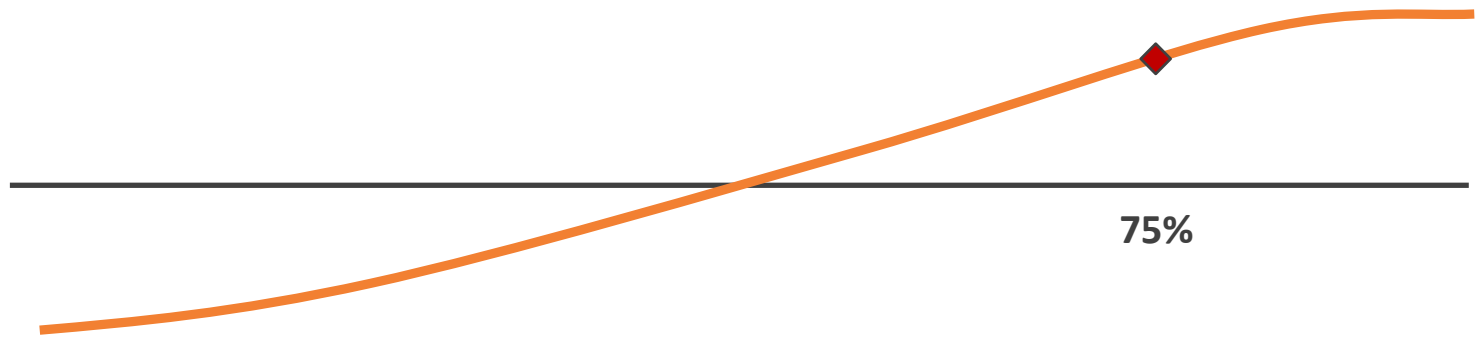




# Time series – how does it work?

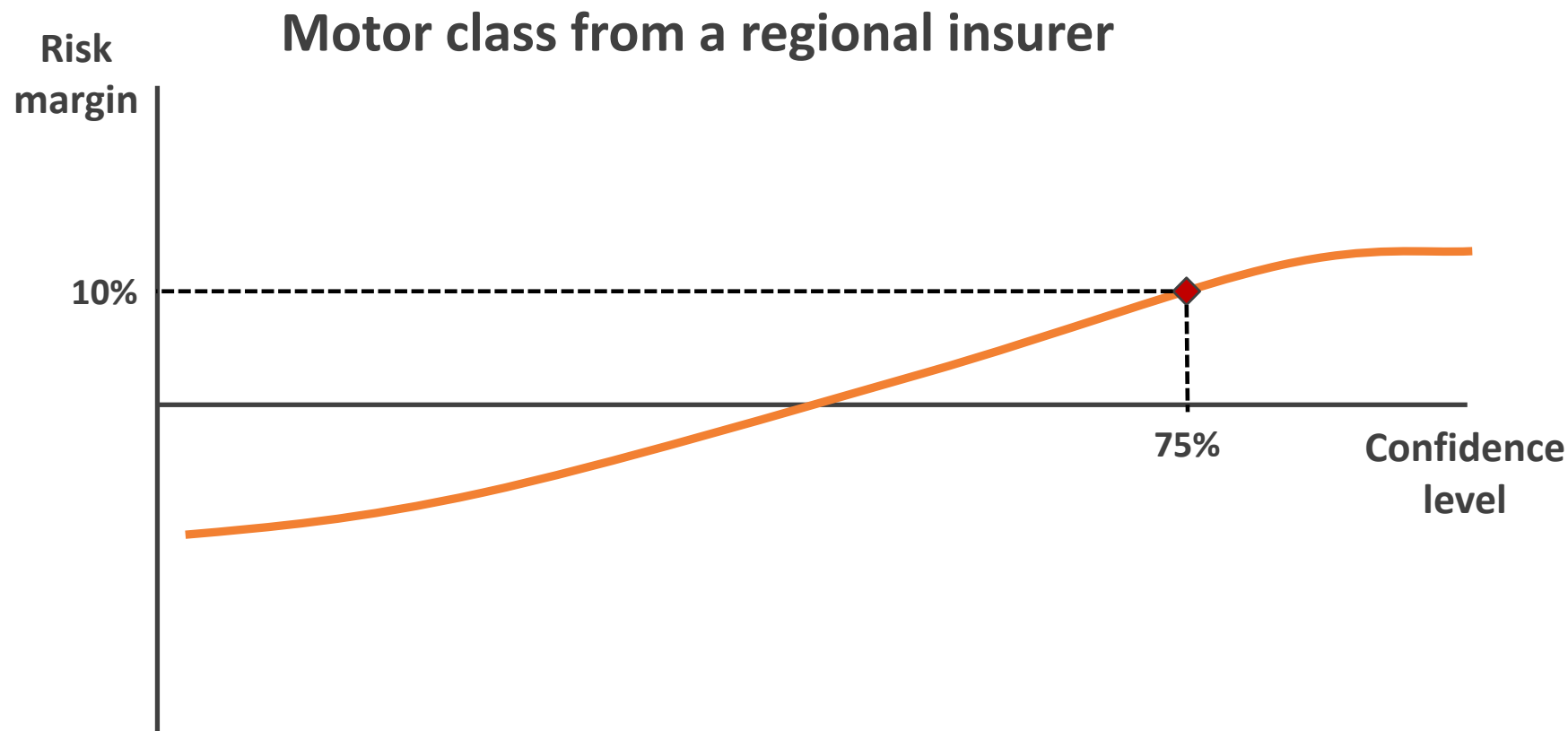
**Step 5:** Determine the 75<sup>th</sup> percentile

## Motor class from a regional insurer



## Time series – how does it work?

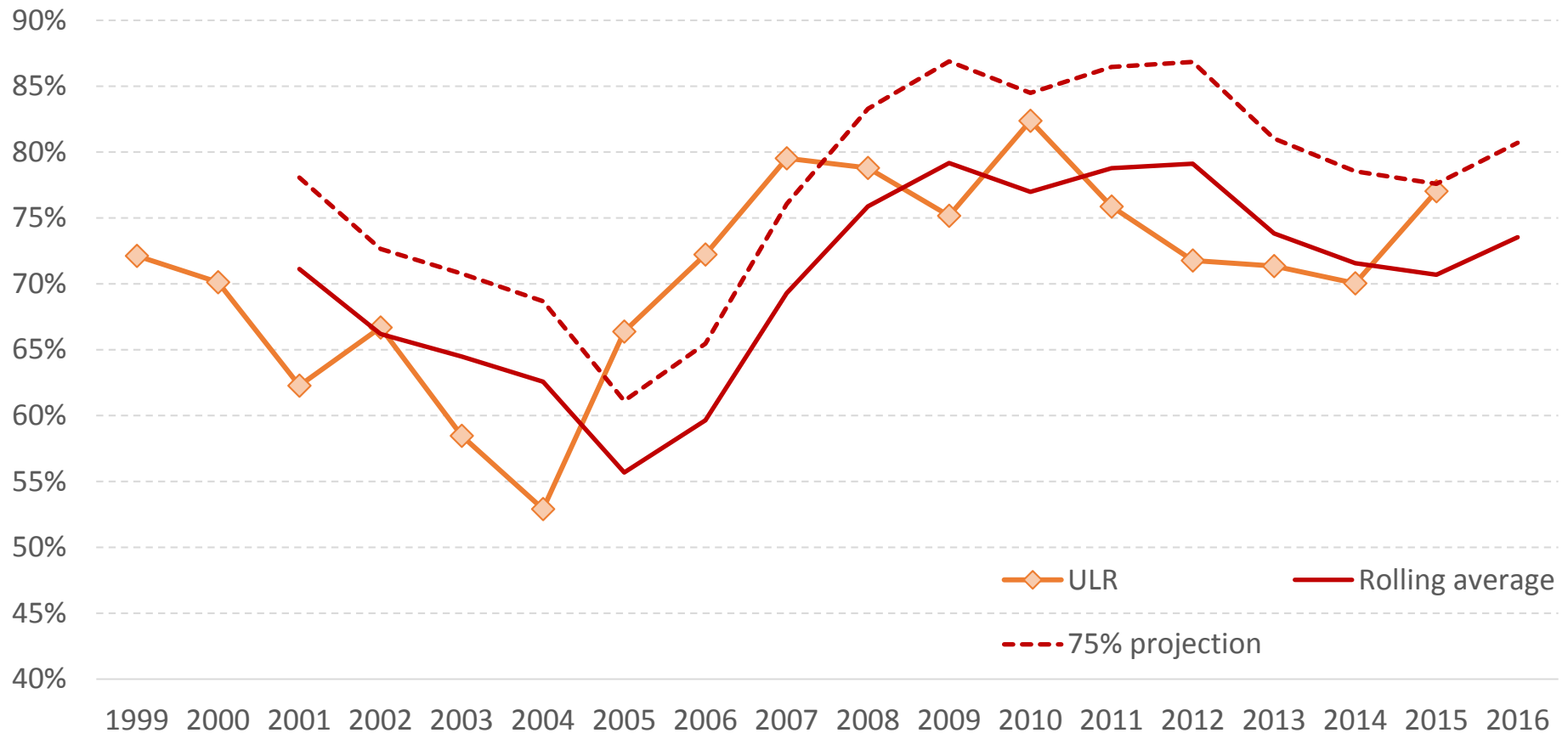
**Step 6:** Calculate the 75% risk margin from the trendline



# Time series – how does it work?

## Step 7: Calculate the 75% URR loss ratio

### Motor class from a regional insurer

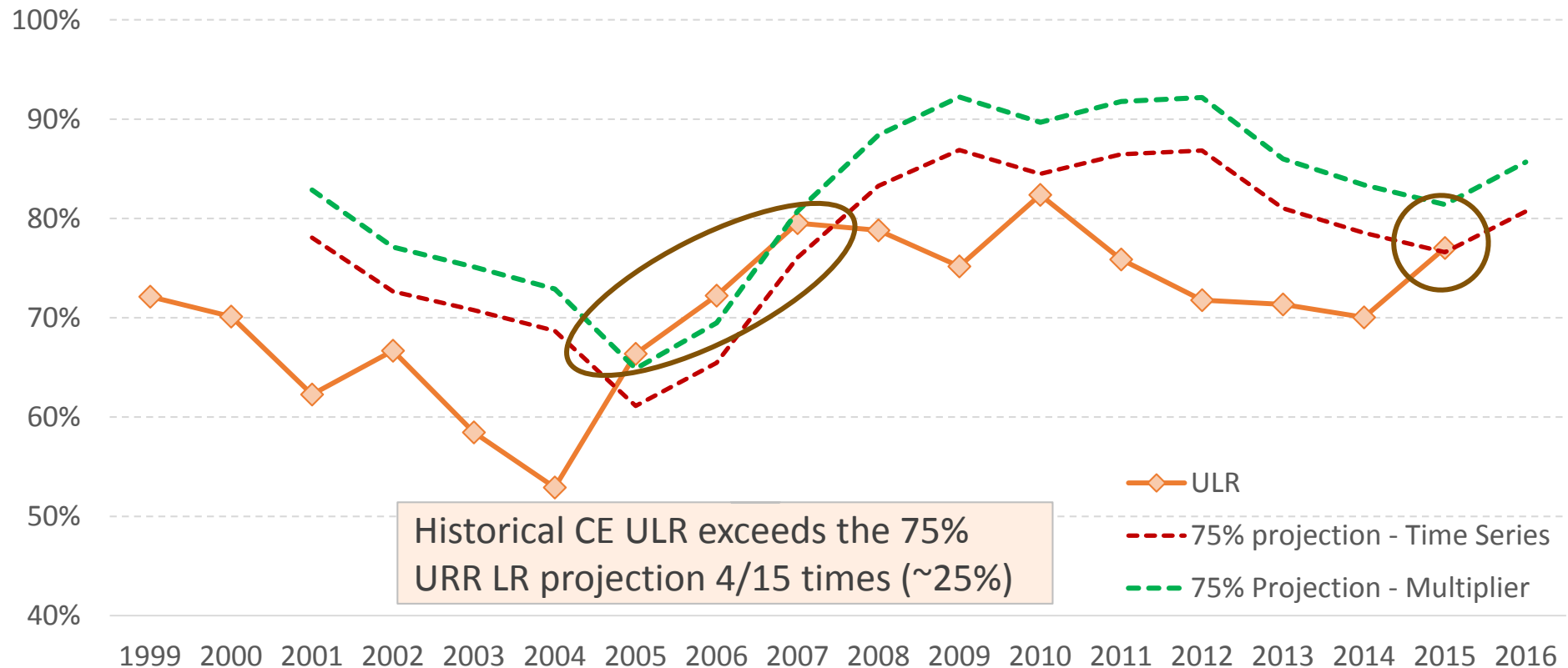


# Comparison of methods – Time series vs Multiplier

Stochastic Chain Ladder suggests the Claim Liability risk margin to be 11%

	Time Series	Multiplier @ 1.5
Loadings	10%	16.5%

## Motor class from a regional insurer

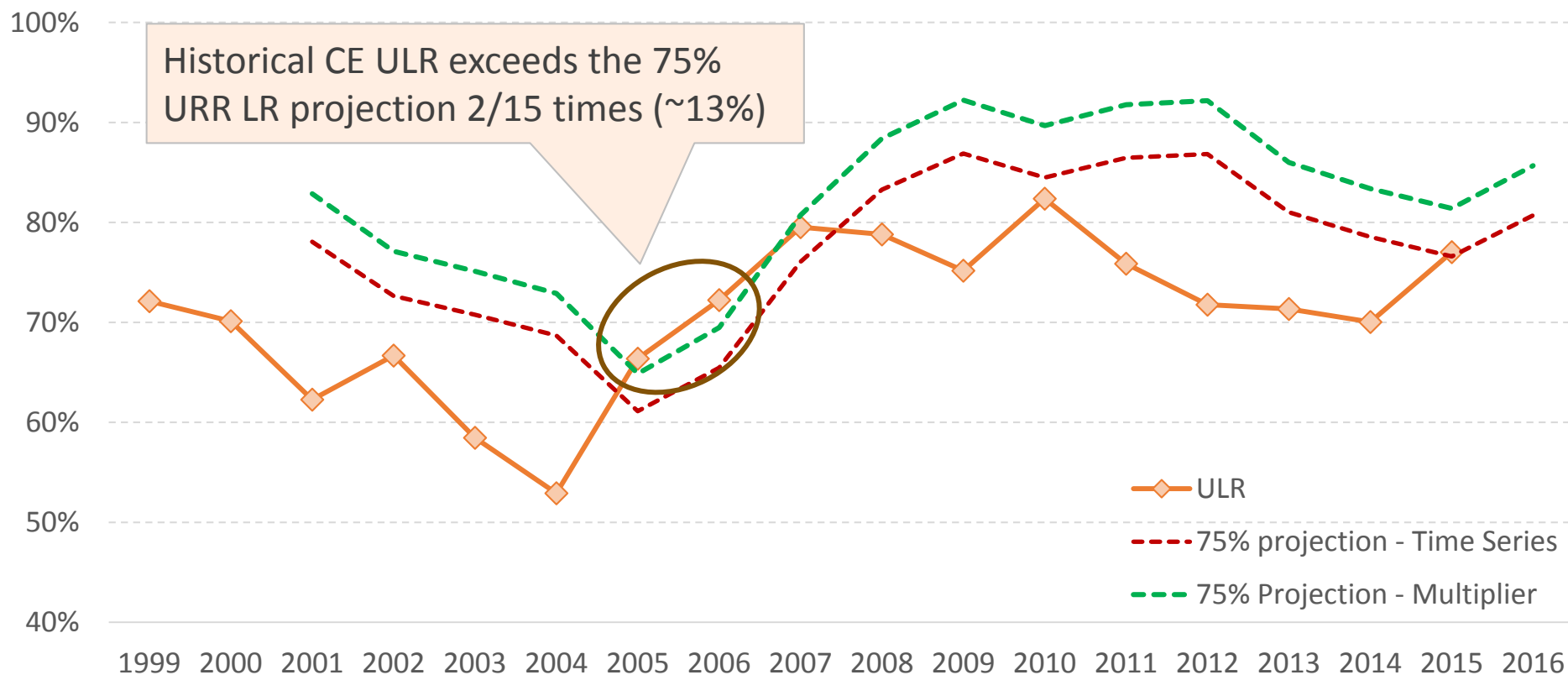


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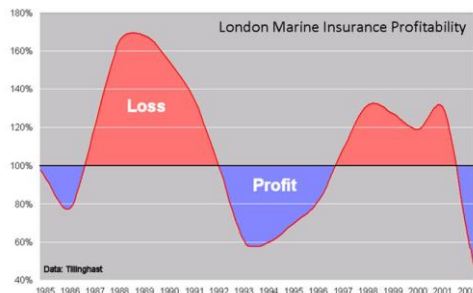
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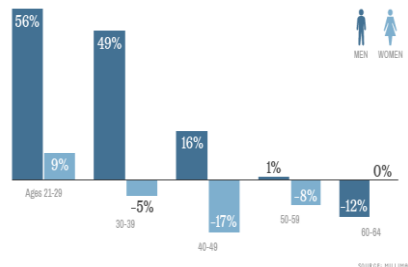


# Variations of Time series

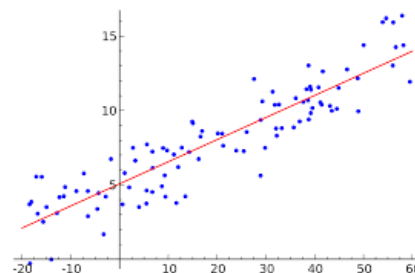
## Other considerations



Underwriting cycle



Change in premium rates



Detailed regression?



Amount of data

## Other structures

- Reducing weights to older values
- Linear extrapolation of prior values
- Long-Term Average
- Moving Average with Mean Reversion
- Linear extrapolation with Mean Reversion
- Adjustments for changes in historical average premium

**Goodness  
of Fit**

# Summary

## Claim Liability

## Premium Liability

### Volatility drivers

- Claims settlement process
- Claims experience

### Current methodologies employed

- Industry benchmark and Judgement are regulators' and auditors' least favourite
- Mack and Bootstrap have no relationship to the Central Estimate selected
- Adding a loading to the Claim Liability risk margin to determine the Premium Liability's is too simplistic

### Recommended approach

- Stochastic Chain Ladder
- Time Series

### Comments

- Continuous enhancements are required
- Loadings for Premium Liability can be lower than Claim Liability

What's next?

“We never finish our App,  
we just release it”



# Thank you

***“Shape your thinking on the decisions that matter. Our specialist focus, global insights programmes and unique network give us the inside track in insurance and investment markets. We translate insights into opportunities.”***

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shape your thinking