

## CONTINUOUS MORTALITY INVESTIGATION: ASSURED LIVES 1944-1948

THE last note published on the assured lives experience appeared in *J.I.A.* LXXII, 516 and *T.F.A.* XVIII, 167, and related to the period 1939-43. Statistics are now available for 1944-48 and are, perhaps, of more interest than usual because the last two years of this period, being free from the disturbing feature of war mortality, afford an opportunity of assessing the effects on the assured lives experience of the decline in mortality that has occurred in recent years.

### 1. PUBLICATION OF BASIC DATA

Statistics are in course of publication giving for each year of the period 1944-48 the 'in force' and 'deaths' at each age for each year of duration 0 to 4 and for durations 5 and over. The particulars will be given separately for the medical and non-medical sections and for each of the four classes of assurance. These statistics will be in a different form from those published for the first twenty years of the investigation, which consisted of 'exposed to risk' and 'deaths' for quinquennial periods but not for individual calendar years. With statistics in the new form it will be possible for anyone to investigate the mortality experience in any one of the five years 1944-48. In future it is intended to publish similar statistics year by year.

### 2. CHARTS ILLUSTRATING SECULAR TREND

In order that the contributing offices might have some broad indication of mortality changes from year to year since the beginning of the continuous investigation, a series of graphs has recently been sent to them illustrating in quinary age-groups the rates of mortality, for durations 5 and over, experienced in each calendar year from 1924 to 1948 inclusive by all classes of assured lives (medical and non-medical) combined. The group rates of mortality on which the graphs were based are given in Appendix I of this note.

### 3. RATES OF MORTALITY DURING THE PERIOD

Following the precedent established in earlier notes, rates of mortality in quinary age-groups for durations 0, 1 and 2, and for combined durations 3 and over, have been calculated for the quinquennium 1944-48 and are reproduced in Appendix II. This information is given separately for medical and non-medical business and is subdivided according to the four standard classes of policy. In order to indicate the weight of the statistics on which the mortality rates are based, the actual deaths are also shown in the tables.

The most significant and interesting information is that which relates to the post-war years 1947 and 1948. Tables corresponding to those in Appendix II have therefore been prepared for these two years combined and are to be found in Appendix III.

## 4. RATIOS OF ACTUAL TO EXPECTED DEATHS

In accordance with customary practice a table has been prepared, and is reproduced in Appendix IV, showing ratios of actual deaths to those expected by the A 1924-29 table in various groups of assured lives for each year of the period under review. These groups are not standardized for age and, in view of variations in the age distribution between one group and another, caution is required when interpreting the resultant ratios. Thus, the 'in force' under non-medical business has a much younger age-distribution than under medical business. As the proportionate improvement over the A 1924-29 table has been greatest at young ages, it is to be expected that the over-all ratio for non-medical business would be lower than for medical business. And in fact this was so for the post-war years, that is to say when the effects of war mortality had ceased to operate. For the war years the heavy toll of the war on young lives produced a contrary result. In neither case, however, do the over-all ratios provide a reliable guide to the relative mortality of medical and non-medical business. Similar considerations apply to comparisons between any other of the groups into which the data are divided.

It is hoped in future notes on the mortality of assured lives to avoid the shortcomings of Appendix IV by presenting a closer analysis of each class of assurance. Improved methods of comparison are now under consideration by the Joint Mortality Committee.

## 5. CURRENT LEVEL OF ASSURED LIVES MORTALITY

In order to give some general indication of the current level of the mortality of assured lives, the data for all classes of business at durations 3 and over have been combined for the two years 1947-48 and a set of mortality rates has been derived. The rates were graduated by Spencer's 21-term formula, with adjustments at the young and old ages, and a comparison between the resultant values of  $q_x$  and the corresponding values from the A 1924-29 ultimate table will be found in Appendix V.

Inspection of these results reveals some interesting features. The ratios in the final column, while showing a broad tendency to increase with advancing age, do not by any means progress uniformly. In fact, the relative improvement at age 40 is greater than at age 20; and at age 70 it is greater than it is anywhere over the range 50-65. A graph of these ratios is reproduced in Appendix V.

On a general over-all view it may be said that for purposes of summarizing current mortality in relation to the A 1924-29 table, the data may be divided into three broad age-groups, viz. under 45, 45-74 and 75 and over. In the first of these groups current experience is about 60 % of the A 1924-29 table; in the second group it is about 80 %; and in the third group it approximates to 90 %.

## 6. MONETARY EFFECTS OF IMPROVED MORTALITY

The Committee is of the opinion that the experience of a few more post-war years should be collected before new tables are prepared for general use. But in order to give some indication of the monetary effect of the marked changes

in mortality during the past twenty years, annuity and assurance values and pure premiums have been calculated on a 3 % basis on the graduated mortality rates for 1947-48 described in section 5. They are reproduced in the table in Appendix VI and the corresponding A1924-29 ultimate values are shown alongside for comparison.

## 7. MORTALITY INDICES FOR INDIVIDUAL OFFICES

It will be evident, from what has already been said with regard to the relative improvement in mortality at different ages, that, owing to the differences between the age distributions of individual offices, no valid comparison can be made between the over-all ratio of actual to expected deaths for any particular office and the corresponding ratio for all offices combined. The Committee is therefore considering alternative methods of giving offices a broad indication of how their mortality compares with the general experience, and it is hoped in due course to evolve suitable indices for this purpose.

## 8. CHILDREN'S DEFERRED ASSURANCES

The data for the five years 1944-48 are shown in the following table:

Children's deferred assurances

| Calendar year | Exposed to risk | Actual deaths | Expected deaths by A1924-29 ultimate | (A - E)/E % |
|---------------|-----------------|---------------|--------------------------------------|-------------|
| 1944          | 23,373          | 366           | 66                                   | +455        |
| 1945          | 25,238          | 289           | 71                                   | +307        |
| 1946          | 27,100          | 117           | 78                                   | +50         |
| 1947          | 29,778          | 63            | 86                                   | -27         |
| 1948          | 32,501          | 65            | 95                                   | -32         |
| 1944-48       | 137,990         | 900           | 396                                  | +127        |
| 1947-48       | 62,279          | 128           | 181                                  | -29         |

Since most of the lives exposed in this class of assurance are young, war mortality has a very pronounced effect on the ratios of actual to expected deaths for 1944-46. The experience for 1947-48 is analysed in age-groups in the following table, where the actual deaths are compared with those expected on the basis of the experience during the same period for the main classes of assurance at durations 3 and over.

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## Children's deferred assurance

Comparison of the actual deaths with the expected deaths on the basis of the 1947-48 experience of assured lives, durations 3 and over.

| Age-group | Actual deaths | Expected deaths |
|-----------|---------------|-----------------|
| 21-25     | 37            | 38              |
| 26-30     | 34            | 27              |
| 31-35     | 14            | 13              |
| 36-40     | 12            | 13              |
| 41-45     | 12            | 12              |
| 46-50     | 7             | 10              |
| 51-55     | 7             | 5               |
| 56-       | 5             | 4               |
|           | 128           | 122             |

This table suggests that there may be no significant difference between the mortality experience of children's deferred assurances after vesting and that of the main body of assured lives.



Tables of deaths and group rates of mortality

1944-48

Medical

| Age group            | Actual deaths |            |            |            | Group rate of mortality |            |            |                      |
|----------------------|---------------|------------|------------|------------|-------------------------|------------|------------|----------------------|
|                      | Duration 1    |            | Duration 2 |            | Duration 1              |            | Duration 2 |                      |
|                      | Duration 0    | Duration 1 | Duration 0 | Duration 1 | Duration 0              | Duration 1 | Duration 2 | Durations 3 and over |
| Life—with profits    |               |            |            |            |                         |            |            |                      |
| 20½-24½              | 11            | 8          | 8          | 86         | ·00676                  | ·01144     | ·01970     | ·01970               |
| 25½-29½              | 8             | 6          | 10         | 188        | ·00208                  | ·00559     | ·00589     | ·00589               |
| 30½-34½              | 2             | 4          | 4          | 268        | ·00125                  | ·00198     | ·00370     | ·00370               |
| 35½-39½              | 4             | 4          | 6          | 208        | ·00155                  | ·00300     | ·00319     | ·00319               |
| 40½-44½              | 6             | 4          | 6          | 215        | ·00268                  | ·00364     | ·00312     | ·00312               |
| 45½-49½              | 5             | 4          | 3          | 361        | ·00265                  | ·00253     | ·00370     | ·00310               |
| 50½-54½              | 10            | 7          | 6          | 683        | ·00516                  | ·00408     | ·00820     | ·00820               |
| 55½-59½              | 10            | 24         | 25         | 1469       | ·00515                  | ·01415     | ·01358     | ·01358               |
| 60½-64½              | 12            | 22         | 35         | 3022       | ·00840                  | ·00355     | ·02337     | ·02337               |
| 65½-69½              | 7             | 16         | 17         | 5499       | ·01282                  | ·01704     | ·03583     | ·03583               |
| 70½-74½              | —             | 6          | 5          | 7267       | ·00000                  | ·05021     | ·05404     | ·05404               |
| 75½-79½              | 1             | —          | —          | 8207       | ·13333                  | —          | ·08892     | ·08892               |
| 80½-84½              | —             | —          | —          | 6660       | —                       | —          | ·13920     | ·13920               |
| 85½-89½              | —             | —          | —          | 3883       | —                       | —          | ·20815     | ·20815               |
| 90½-94½              | —             | —          | —          | 1157       | —                       | —          | ·27505     | ·27505               |
| 95½-99½              | —             | —          | —          | 183        | —                       | —          | ·31909     | ·31909               |
| 100½—                | —             | —          | —          | 16         | —                       | —          | ·46377     | ·46377               |
| Life—without profits |               |            |            |            |                         |            |            |                      |
| 20½-24½              | 6             | 7          | 6          | 30         | ·00643                  | ·00994     | ·01288     | ·01288               |
| 25½-29½              | 7             | 8          | 7          | 104        | ·00269                  | ·00364     | ·00888     | ·00888               |
| 30½-34½              | 7             | 9          | 2          | 163        | ·00275                  | ·00092     | ·00453     | ·00453               |
| 35½-39½              | —             | 8          | 1          | 178        | ·00267                  | ·00046     | ·00313     | ·00313               |
| 40½-44½              | 3             | 7          | 1          | 200        | ·00290                  | ·00319     | ·00319     | ·00319               |
| 45½-49½              | 6             | 7          | 3          | 350        | ·00422                  | ·00190     | ·00592     | ·00592               |
| 50½-54½              | 4             | 6          | 7          | 487        | ·00393                  | ·00524     | ·00833     | ·00833               |
| 55½-59½              | 5             | 15         | 10         | 835        | ·01278                  | ·00786     | ·01350     | ·01350               |
| 60½-64½              | 3             | 12         | 14         | 1310       | ·01556                  | ·01580     | ·02157     | ·02157               |
| 65½-69½              | —             | 3          | 6          | 1710       | ·01040                  | ·01613     | ·03275     | ·03275               |
| 70½-74½              | —             | 1          | 2          | 1875       | ·01852                  | ·02597     | ·05001     | ·05001               |
| 75½-79½              | —             | —          | —          | 1619       | —                       | —          | ·08063     | ·08063               |
| 80½-84½              | —             | —          | —          | 982        | —                       | —          | ·12548     | ·12548               |
| 85½-89½              | —             | —          | —          | 166        | —                       | —          | ·20815     | ·20815               |

| Endowment assurance—with profits    |    |     |     |      |        |        |        |        |  |
|-------------------------------------|----|-----|-----|------|--------|--------|--------|--------|--|
| 20½-24½                             | 82 | 75  | 83  | 501  | ·00218 | ·00344 | ·00579 | ·00662 |  |
| 25½-29½                             | 54 | 58  | 59  | 1114 | ·00095 | ·00145 | ·00249 | ·00647 |  |
| 30½-34½                             | 47 | 44  | 43  | 1658 | ·00076 | ·00095 | ·00144 | ·00407 |  |
| 35½-39½                             | 53 | 54  | 55  | 1623 | ·00088 | ·00128 | ·00162 | ·00259 |  |
| 40½-44½                             | 74 | 95  | 84  | 2178 | ·00156 | ·00230 | ·00258 | ·00310 |  |
| 45½-49½                             | 66 | 78  | 102 | 3046 | ·00216 | ·00277 | ·00398 | ·00481 |  |
| 50½-54½                             | 85 | 101 | 117 | 4195 | ·00399 | ·00470 | ·00554 | ·00781 |  |
| 55½-59½                             | 64 | 85  | 105 | 5169 | ·00726 | ·00843 | ·00880 | ·01244 |  |
| 60½-64½                             | 36 | 35  | 55  | 4339 | ·01216 | ·00998 | ·01292 | ·01889 |  |
| 65½-69½                             | 13 | 20  | 35  | 1981 | ·01657 | ·01848 | ·02533 | ·02898 |  |
| 70½-74½                             | 2  | 1   | 4   | 576  | ·05797 | ·01242 | ·02721 | ·04133 |  |
| 75½-79½                             | —  | —   | —   | 74   | —      | —      | —      | ·05638 |  |
| 80½—                                | —  | —   | —   | 10   | —      | —      | —      | ·04926 |  |
| Endowment assurance—without profits |    |     |     |      |        |        |        |        |  |
| 20½-24½                             | 4  | 14  | 20  | 68   | ·00083 | ·00477 | ·00764 | ·00611 |  |
| 25½-29½                             | 6  | 16  | 19  | 156  | ·00049 | ·00201 | ·00360 | ·00611 |  |
| 30½-34½                             | 27 | 24  | 24  | 208  | ·00154 | ·00192 | ·00263 | ·00329 |  |
| 35½-39½                             | 12 | 19  | 22  | 253  | ·00067 | ·00134 | ·00188 | ·00228 |  |
| 40½-44½                             | 19 | 16  | 26  | 353  | ·00142 | ·00137 | ·00238 | ·00263 |  |
| 45½-49½                             | 16 | 31  | 29  | 607  | ·00196 | ·00385 | ·00344 | ·00484 |  |
| 50½-54½                             | 25 | 21  | 39  | 792  | ·00485 | ·00372 | ·00578 | ·00738 |  |
| 55½-59½                             | 5  | 14  | 31  | 847  | ·00279 | ·00568 | ·00855 | ·01111 |  |
| 60½-64½                             | 5  | 9   | 12  | 579  | ·01264 | ·01354 | ·01054 | ·01651 |  |
| 65½-69½                             | 1  | 1   | 9   | 213  | ·01504 | ·00735 | ·03303 | ·02500 |  |
| 70½-74½                             | —  | —   | —   | 60   | —      | —      | —      | ·03727 |  |
| 75½—                                | —  | —   | —   | 12   | —      | —      | —      | ·04958 |  |

Note. In each column the last rate of mortality shown is the group rate applicable to all ages for which there are exposed to risk from the youngest age in that group upwards.

## APPENDIX II (cont.)

## Tables of deaths and group rates of mortality

1944-48

Non-medical

| Age-group            | Actual deaths |            |            |                      | Group rate of mortality |            |                     |                      |
|----------------------|---------------|------------|------------|----------------------|-------------------------|------------|---------------------|----------------------|
|                      | Duration 0    |            | Duration 1 |                      | Duration 2              |            | Duration 3 and over |                      |
|                      | Duration 0    | Duration 1 | Duration 2 | Durations 3 and over | Duration 0              | Duration 1 | Duration 2          | Durations 3 and over |
| Life—with profits    |               |            |            |                      |                         |            |                     |                      |
| 20-24½               | 5             | 3          | 3          | 25                   | ·00384                  | ·00480     | ·00770              | ·01750               |
| 25-29½               | 2             | 4          | 8          | 58                   | ·00108                  | ·00302     | ·00941              | ·00820               |
| 30-34½               | 4             | 3          | 3          | 148                  | ·00212                  | ·00209     | ·00314              | ·00734               |
| 35-39½               | —             | 3          | 3          | 84                   | ·00000                  | ·00219     | ·00278              | ·00257               |
| 40-44½               | 3             | 1          | 3          | 109                  | ·00228                  | ·00082     | ·00297              | ·00310               |
| 45-49½               | 2             | 1          | 7          | 163                  | ·00340                  | ·00148     | ·01075              | ·00553               |
| 50-54½               | 2             | 2          | 3          | 239                  | ·00661                  | ·00563     | ·00766              | ·00906               |
| 55-59½               | 2             | 6          | 2          | 396                  | ·01055                  | ·02395     | ·00758              | ·01534               |
| 60-64½               | 4             | 2          | 1          | 470                  | ·03791                  | ·01613     | ·00719              | ·02171               |
| 65-69½               | 1             | 1          | 4          | 548                  | ·06250                  | ·02298     | ·06154              | ·03682               |
| 70-74½               | —             | 1          | —          | 512                  | —                       | ·28571     | —                   | ·05287               |
| 75-79½               | —             | —          | —          | 524                  | —                       | —          | —                   | ·10258               |
| 80-84½               | —             | —          | —          | 270                  | —                       | —          | —                   | ·13889               |
| 85-89½               | —             | —          | —          | 107                  | —                       | —          | —                   | ·18838               |
| 90-94½               | —             | —          | —          | 31                   | —                       | —          | —                   | ·25203               |
| 95-99½               | —             | —          | —          | 7                    | —                       | —          | —                   | ·32558               |
| Life—without profits |               |            |            |                      |                         |            |                     |                      |
| 20-24½               | 6             | 2          | 2          | 40                   | ·00596                  | ·00409     | ·00556              | ·01772               |
| 25-29½               | 3             | 1          | 5          | 58                   | ·00143                  | ·00080     | ·00736              | ·00848               |
| 30-34½               | 3             | 3          | 2          | 83                   | ·00129                  | ·00190     | ·00190              | ·00420               |
| 35-39½               | 2             | 5          | 2          | 82                   | ·00096                  | ·00315     | ·00164              | ·00265               |
| 40-44½               | 1             | 1          | 6          | 106                  | ·00065                  | ·00081     | ·00372              | ·00338               |
| 45-49½               | 1             | 4          | 2          | 137                  | ·00146                  | ·00560     | ·00272              | ·00506               |
| 50-54½               | 1             | 2          | 4          | 172                  | ·00515                  | ·00748     | ·01120              | ·00803               |
| 55-59½               | —             | 3          | 2          | 220                  | ·00000                  | ·01161     | ·01163              | ·01306               |
| 60-64½               | 1             | —          | 1          | 214                  | ·01739                  | —          | ·01058              | ·02180               |
| 65-69½               | 2             | —          | 1          | 176                  | ·18182                  | —          | ·03151              | ·05752               |
| 70-74½               | —             | —          | —          | 185                  | —                       | —          | ·02564              | ·08471               |
| 75-79½               | —             | —          | —          | 126                  | —                       | —          | —                   | ·13176               |
| 80-84½               | —             | —          | —          | 56                   | —                       | —          | —                   | —                    |

| Endowment assurance—with profits    |     |     |     |      |       |       |       |       |  |
|-------------------------------------|-----|-----|-----|------|-------|-------|-------|-------|--|
| 20½-24½                             | 170 | 152 | 240 | 1257 | 00230 | 00313 | 00597 | 00734 |  |
| 25-29½                              | 104 | 137 | 109 | 2041 | 00129 | 00230 | 00279 | 00307 |  |
| 30-34½                              | 80  | 110 | 118 | 2256 | 00101 | 00175 | 00252 | 00352 |  |
| 35-39½                              | 109 | 136 | 102 | 2196 | 00135 | 00198 | 00182 | 00261 |  |
| 40-44½                              | 134 | 158 | 182 | 2894 | 00192 | 00242 | 00300 | 00324 |  |
| 45-49½                              | 106 | 172 | 190 | 3957 | 00247 | 00388 | 00435 | 00510 |  |
| 50-54½                              | 65  | 129 | 159 | 4707 | 00404 | 00640 | 00704 | 00823 |  |
| 55-59½                              | 49  | 71  | 111 | 5072 | 00683 | 00798 | 01144 | 01358 |  |
| 60-64½                              | 12  | 45  | 57  | 3016 | 00622 | 01540 | 01561 | 02075 |  |
| 65-69½                              | 5   | 6   | 15  | 857  | 03390 | 01338 | 01934 | 03097 |  |
| 70-74½                              | 1   | —   | —   | 181  | 13333 | —     | —     | 04502 |  |
| 75-79½                              | —   | —   | —   | 35   | —     | —     | —     | 08692 |  |
| 80½                                 | —   | —   | —   | 2    | —     | —     | —     | 03333 |  |
| Endowment assurance—without profits |     |     |     |      |       |       |       |       |  |
| 20½-24½                             | 12  | 10  | 17  | 144  | 00247 | 00357 | 00629 | 00857 |  |
| 25-29½                              | 14  | 10  | 7   | 190  | 00166 | 00511 | 00223 | 00581 |  |
| 30-34½                              | 8   | 9   | 11  | 290  | 00076 | 00126 | 00225 | 00421 |  |
| 35-39½                              | 19  | 15  | 6   | 264  | 00189 | 00198 | 00102 | 00246 |  |
| 40-44½                              | 12  | 13  | 12  | 348  | 00157 | 00202 | 00215 | 00291 |  |
| 45-49½                              | 11  | 15  | 13  | 496  | 00276 | 00401 | 00347 | 00483 |  |
| 50-54½                              | 7   | 4   | 12  | 529  | 00645 | 00314 | 00805 | 00757 |  |
| 55-59½                              | 4   | 5   | 2   | 498  | 00728 | 01198 | 00565 | 01274 |  |
| 60-64½                              | —   | 3   | 4   | 256  | —     | 03614 | 04020 | 02196 |  |
| 65-69½                              | —   | 1   | —   | 28   | —     | 06250 | —     | 02692 |  |
| 70-74½                              | —   | —   | —   | 7    | —     | —     | —     | 04620 |  |
| 75-79½                              | —   | —   | —   | 3    | —     | —     | —     | 08955 |  |

Note. In each column the last rate of mortality shown is the group rate applicable to all ages for which there are exposed to risk from the youngest age in that group upwards.

## APPENDIX III

## Tables of deaths and group rates of mortality

1947-48

Medical

| Age group            | Actual deaths |            |            |                      | Group rate of mortality |            |            |                      |
|----------------------|---------------|------------|------------|----------------------|-------------------------|------------|------------|----------------------|
|                      | Duration 0    | Duration 1 | Duration 2 | Durations 3 and over | Duration 0              | Duration 1 | Duration 2 | Durations 3 and over |
| Life—without profits |               |            |            |                      |                         |            |            |                      |
| 20½-24½              | 1             | 1          | —          | —                    | ·00069                  | ·00140     | ·00000     | ·00000               |
| 25½-29½              | 5             | 1          | 1          | 9                    | ·00194                  | ·00049     | ·00104     | ·00182               |
| 30½-34½              | 1             | 3          | 2          | 19                   | ·00040                  | ·00132     | ·00174     | ·00127               |
| 35½-39½              | 1             | 2          | 2          | 49                   | ·00054                  | ·00123     | ·00194     | ·00204               |
| 40½-44½              | 3             | 4          | 1          | 72                   | ·00249                  | ·00356     | ·00126     | ·00266               |
| 45½-49½              | 4             | 2          | —          | 128                  | ·00387                  | ·00242     | ·00000     | ·00456               |
| 50½-54½              | 7             | 5          | 5          | 231                  | ·00767                  | ·00648     | ·00844     | ·00759               |
| 55½-59½              | 2             | 10         | 13         | 557                  | ·00219                  | ·01253     | ·01935     | ·01407               |
| 60½-64½              | 4             | 5          | 14         | 1116                 | ·00662                  | ·00797     | ·02324     | ·02249               |
| 65½-69½              | 1             | 3          | 7          | 2139                 | ·00458                  | ·01045     | ·02137     | ·03707               |
| 70½-74½              | —             | 3          | 1          | 2830                 | ·00000                  | ·05714     | ·01626     | ·05308               |
| 75½-79½              | 1             | —          | —          | 3240                 | ·22222                  | —          | —          | ·08768               |
| 80½-84½              | —             | —          | —          | 2629                 | —                       | —          | —          | ·13845               |
| 85½-89½              | —             | —          | —          | 1474                 | —                       | —          | —          | ·19822               |
| 90½-94½              | —             | —          | —          | 460                  | —                       | —          | —          | ·20590               |
| 95½-99½              | —             | —          | —          | 73                   | —                       | —          | —          | ·33032               |
| 100½—                | —             | —          | —          | 6                    | —                       | —          | —          | ·40000               |
| Life—without profits |               |            |            |                      |                         |            |            |                      |
| 20½-24½              | 1             | 1          | 1          | 1                    | ·00074                  | ·00164     | ·00418     | ·00157               |
| 25½-29½              | —             | 1          | —          | 8                    | ·00000                  | ·00051     | ·00000     | ·00259               |
| 30½-34½              | 4             | 5          | —          | 14                   | ·00136                  | ·00223     | ·00000     | ·00132               |
| 35½-39½              | —             | 4          | 1          | 46                   | ·00000                  | ·00208     | ·00007     | ·00224               |
| 40½-44½              | 1             | 3          | —          | 75                   | ·00062                  | ·00214     | ·00000     | ·00298               |
| 45½-49½              | 3             | 5          | 2          | 138                  | ·00269                  | ·00571     | ·00315     | ·00564               |
| 50½-54½              | 4             | 2          | 1          | 193                  | ·00458                  | ·00263     | ·00190     | ·00833               |
| 55½-59½              | 1             | 7          | 4          | 303                  | ·00171                  | ·01417     | ·00898     | ·01243               |
| 60½-64½              | 2             | 2          | 3          | 522                  | ·00716                  | ·00673     | ·01107     | ·02152               |
| 65½-69½              | 1             | 1          | 3          | 773                  | ·00939                  | ·00758     | ·02055     | ·03580               |
| 70½-74½              | —             | —          | —          | 796                  | —                       | —          | —          | ·05000               |
| 75½-79½              | —             | —          | —          | 719                  | —                       | —          | —          | ·08082               |

| Endowment assurance—with profits    |    |    |    |      |       |       |       |       |  |
|-------------------------------------|----|----|----|------|-------|-------|-------|-------|--|
| 20½-24½                             | 23 | 20 | 8  | 29   | 00096 | 00155 | 00122 | 00161 |  |
| 25½-29½                             | 21 | 19 | 12 | 79   | 00057 | 00066 | 00084 | 00140 |  |
| 30½-34½                             | 24 | 18 | 23 | 205  | 00063 | 00057 | 00141 | 00145 |  |
| 35½-39½                             | 30 | 33 | 22 | 449  | 00083 | 00109 | 00123 | 00188 |  |
| 40½-44½                             | 45 | 57 | 38 | 787  | 00169 | 00239 | 00230 | 00277 |  |
| 45½-49½                             | 42 | 42 | 49 | 1265 | 00259 | 00282 | 00416 | 00479 |  |
| 50½-54½                             | 44 | 44 | 44 | 1699 | 00437 | 00437 | 00520 | 00763 |  |
| 55½-59½                             | 30 | 33 | 42 | 2188 | 00703 | 00781 | 00923 | 01262 |  |
| 60½-64½                             | 14 | 16 | 17 | 1913 | 01023 | 01106 | 01060 | 02019 |  |
| 65½-69½                             | 9  | 5  | 8  | 835  | 02727 | 01193 | 01467 | 02021 |  |
| 70½-74½                             | 1  | 1  | 1  | 258  | 07692 | 03030 | 01527 | 04388 |  |
| 75½-79½                             | —  | —  | —  | 24   | —     | —     | —     | 03880 |  |
| 80½—                                | —  | —  | —  | 7    | —     | —     | —     | 09389 |  |
| Endowment assurance—without profits |    |    |    |      |       |       |       |       |  |
| 20½-24½                             | 1  | 1  | 1  | 6    | 00033 | 00079 | 00154 | 00141 |  |
| 25½-29½                             | 2  | 5  | 1  | 16   | 00024 | 00098 | 00047 | 00162 |  |
| 30½-34½                             | 14 | 7  | 6  | 36   | 00121 | 00090 | 00061 | 00153 |  |
| 35½-39½                             | 11 | 7  | 9  | 74   | 00096 | 00084 | 00195 | 00165 |  |
| 40½-44½                             | 9  | 8  | 7  | 148  | 00110 | 00128 | 00176 | 00259 |  |
| 45½-49½                             | 6  | 14 | 7  | 262  | 00131 | 00377 | 00252 | 00473 |  |
| 50½-54½                             | 11 | 6  | 10 | 345  | 00425 | 00273 | 00532 | 00735 |  |
| 55½-59½                             | 3  | 3  | 10 | 393  | 00352 | 00353 | 01074 | 01129 |  |
| 60½-64½                             | 1  | 2  | 5  | 267  | 00613 | 00832 | 01988 | 01648 |  |
| 65½-69½                             | 1  | —  | 3  | 97   | 04762 | —     | 05217 | 02339 |  |
| 70½-74½                             | —  | —  | —  | 36   | —     | —     | —     | 04797 |  |
| 75½—                                | —  | —  | —  | 3    | —     | —     | —     | 02970 |  |

Note. In each column the last rate of mortality shown is the group rate applicable to all ages for which there are exposed to risk from the youngest age in that group upwards.

## APPENDIX III (cont.)

## Tables of deaths and group rates of mortality

1947-48

Non-medical

| Age group            | Actual deaths |            |            | Group rate of mortality |            |            |            |                     |
|----------------------|---------------|------------|------------|-------------------------|------------|------------|------------|---------------------|
|                      | Duration 0    | Duration 1 | Duration 2 | Duration 3 and over     | Duration 0 | Duration 1 |            |                     |
|                      |               |            |            |                         |            |            | Duration 2 | Duration 3 and over |
| Life—with profits    |               |            |            |                         |            |            |            |                     |
| 20½-24½              | —             | 3          | —          | 2                       | ·00000     | ·00794     | ·00000     | ·00471              |
| 25½-29½              | —             | —          | 2          | 4                       | ·00000     | ·00000     | ·00458     | ·00212              |
| 30½-34½              | 2             | 3          | 1          | 13                      | ·00174     | ·00302     | ·00206     | ·00210              |
| 35½-39½              | —             | 1          | 2          | 22                      | ·00000     | ·00112     | ·00374     | ·00181              |
| 40½-44½              | 3             | —          | 2          | 48                      | ·00428     | ·00000     | ·00415     | ·00331              |
| 45½-49½              | —             | —          | 4          | 82                      | ·00000     | ·00000     | ·01242     | ·00645              |
| 50½-54½              | —             | 1          | 1          | 89                      | ·00000     | ·00587     | ·00662     | ·00832              |
| 55½-59½              | 1             | 3          | 2          | 175                     | ·00000     | ·02913     | ·01843     | ·01703              |
| 60½-64½              | 1             | 1          | 1          | 200                     | ·04651     | ·01786     | ·01739     | ·02178              |
| 65½-69½              | 1             | —          | 1          | 220                     | ·33333     | —          | ·04444     | ·03427              |
| 70½-74½              | —             | —          | —          | 229                     | —          | —          | —          | ·05544              |
| 75½-79½              | —             | —          | —          | 210                     | —          | —          | —          | ·09894              |
| 80½-84½              | —             | —          | —          | 117                     | —          | —          | —          | ·14063              |
| 85½-89½              | —             | —          | —          | 47                      | —          | —          | —          | ·18112              |
| 90½-94½              | —             | —          | —          | 14                      | —          | —          | —          | ·32184              |
| 95½                  | —             | —          | —          | 1                       | —          | —          | —          | ·11111              |
| Life—without profits |               |            |            |                         |            |            |            |                     |
| 20½-24½              | 1             | —          | —          | 6                       | ·00131     | ·00000     | ·00000     | ·01060              |
| 25½-29½              | 1             | —          | 1          | 5                       | ·00064     | ·00000     | ·00297     | ·00263              |
| 30½-34½              | 2             | 3          | —          | 9                       | ·00122     | ·00262     | ·00000     | ·00158              |
| 35½-39½              | 1             | 2          | 1          | 10                      | ·00071     | ·00185     | ·00183     | ·00086              |
| 40½-44½              | 1             | 1          | —          | 42                      | ·00063     | ·00130     | ·00000     | ·00324              |
| 45½-49½              | —             | 3          | 1          | 47                      | —          | ·00808     | ·00370     | ·00406              |
| 50½-54½              | —             | 1          | 1          | 60                      | —          | ·00758     | ·00823     | ·00647              |
| 55½-59½              | —             | 1          | 2          | 100                     | —          | ·00784     | ·03419     | ·01431              |
| 60½-64½              | —             | —          | 1          | 93                      | —          | —          | ·02247     | ·02086              |
| 65½-69½              | —             | —          | —          | 72                      | —          | —          | —          | ·02838              |
| 70½-74½              | —             | —          | —          | 78                      | —          | —          | —          | ·05520              |
| 75½-79½              | —             | —          | —          | 56                      | —          | —          | —          | ·08396              |

## Endowment assurance—with profits

|         |    |    |    |      |        |        |        |        |
|---------|----|----|----|------|--------|--------|--------|--------|
| 20½-24½ | 35 | 25 | 27 | 112  | ·00076 | ·00095 | ·00171 | ·00174 |
| 25½-29½ | 45 | 51 | 26 | 195  | ·00087 | ·00123 | ·00129 | ·00152 |
| 30½-34½ | 25 | 51 | 32 | 358  | ·00055 | ·00133 | ·00152 | ·00154 |
| 35½-39½ | 42 | 53 | 31 | 637  | ·00097 | ·00140 | ·00129 | ·00192 |
| 40½-44½ | 71 | 73 | 61 | 1094 | ·00203 | ·00226 | ·00249 | ·00299 |
| 45½-49½ | 47 | 89 | 68 | 1662 | ·00228 | ·00424 | ·00370 | ·00489 |
| 50½-54½ | 29 | 60 | 63 | 2013 | ·00404 | ·00677 | ·00669 | ·00819 |
| 55½-59½ | 25 | 28 | 50 | 2095 | ·00838 | ·00736 | ·01258 | ·01342 |
| 60½-64½ | 3  | 11 | 27 | 1218 | ·00425 | ·01001 | ·02020 | ·01993 |
| 65½-69½ | 2  | 3  | 5  | 311  | ·02878 | ·01807 | ·01764 | ·03042 |
| 70½-74½ | —  | —  | —  | 68   | —      | —      | —      | ·04646 |
| 75½-79½ | —  | —  | —  | 14   | —      | —      | —      | ·08777 |
| 80½—    | —  | —  | —  | 2    | —      | —      | —      | ·05970 |

## Endowment assurance—without profits

|         |    |    |   |     |        |        |        |        |
|---------|----|----|---|-----|--------|--------|--------|--------|
| 20½-24½ | 2  | —  | 2 | 12  | ·00060 | ·00000 | ·00234 | ·00197 |
| 25½-29½ | 7  | 1  | 2 | 16  | ·00111 | ·00027 | ·00145 | ·00139 |
| 30½-34½ | 2  | 5  | 3 | 42  | ·00027 | ·00105 | ·00142 | ·00177 |
| 35½-39½ | 11 | 7  | 1 | 66  | ·00161 | ·00145 | ·00040 | ·00159 |
| 40½-44½ | 10 | 7  | 4 | 133 | ·00199 | ·00184 | ·00181 | ·00270 |
| 45½-49½ | 7  | 10 | 7 | 190 | ·00280 | ·00491 | ·00490 | ·00422 |
| 50½-54½ | 6  | 1  | 4 | 222 | ·00860 | ·00144 | ·00694 | ·00709 |
| 55½-59½ | 2  | 3  | 2 | 207 | ·00544 | ·01165 | ·01270 | ·01191 |
| 60½-64½ | —  | 3  | 1 | 128 | —      | ·06000 | ·02105 | ·02377 |
| 65½-69½ | —  | 1  | — | 6   | —      | ·08000 | —      | ·01267 |
| 70½-74½ | —  | —  | — | 4   | —      | —      | —      | ·07143 |
| 75½—    | —  | —  | — | 1   | —      | —      | —      | ·08333 |

Note. In each column the last rate of mortality shown is the group rate applicable to all ages for which there are exposed to risk from the youngest age in that group upwards.

## APPENDIX IV

Table of ratios of actual deaths to those expected by the A1924-29 table

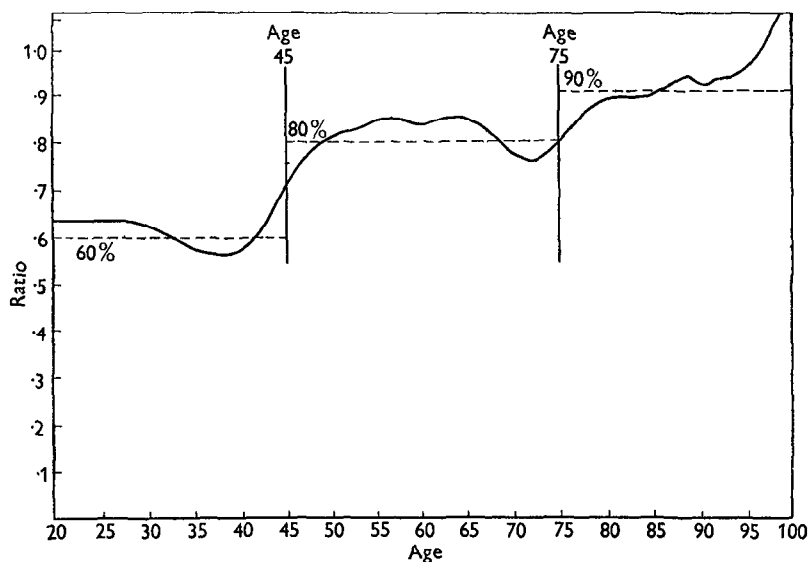
| Class and duration   | Calendar year |       |      |      |      |
|--|---------------|-------|------|------|------|
|  | 1944          | 1945  | 1946 | 1947 | 1948 |
| All classes and durations<br>(Medical and Non-medical)                           | ·999          | ·930  | ·841 | ·810 | ·750 |
| All classes and durations<br>(Medical)   | ·927          | ·867  | ·824 | ·817 | ·759 |
| All classes and durations<br>(Non-medical)                                       | 1·168         | 1·074 | ·879 | ·793 | ·732 |
| Life P.—all durations<br>(Medical)   | ·893          | ·876  | ·898 | ·890 | ·819 |
| Life N.—all durations<br>(Medical)   | ·885          | ·814  | ·807 | ·845 | ·734 |
| E.A.P.—all durations<br>(Medical)  | ·988          | ·889  | ·757 | ·744 | ·715 |
| E.A.N.—all durations<br>(Medical)  | ·939          | ·795  | ·691 | ·661 | ·665 |
| Life P.—all durations<br>(Non-medical)   | 1·042         | ·932  | ·937 | ·966 | ·819 |
| Life N.—all durations<br>(Non-medical)   | 1·045         | 1·016 | ·985 | ·790 | ·726 |
| E.A.P.—all durations<br>(Non-medical)  | 1·182         | 1·100 | ·868 | ·777 | ·734 |
| E.A.N.—all durations<br>(Non-medical)  | 1·243         | 1·017 | ·859 | ·763 | ·631 |
| All classes—durations 0-2<br>(Medical and Non-medical)                           | 1·145         | 1·023 | ·706 | ·613 | ·572 |
| All classes—durations 0-2<br>(Medical)   | ·950          | ·843  | ·655 | ·588 | ·519 |
| All classes—durations 0-2<br>(Non-medical)                                       | 1·341         | 1·200 | ·756 | ·638 | ·626 |
| Life classes—durations 3 and over<br>(Medical)                                   | ·891          | ·862  | ·879 | ·882 | ·802 |
| E.A. classes—durations 3 and over<br>(Medical)                                   | ·984          | ·878  | ·756 | ·748 | ·733 |
| Life classes—durations 3 and over<br>(Non-medical)                               | 1·032         | ·945  | ·952 | ·908 | ·792 |
| E.A. classes—durations 3 and over<br>(Non-medical)                               | 1·170         | 1·082 | ·880 | ·795 | ·739 |
| All classes and all ages—durations<br>5 and over<br>(Medical and Non-medical)    | ·954          | ·919  | ·849 | ·829 | ·773 |
| All classes ages up to 50—durations<br>5 and over<br>(Medical and Non-medical)   | 1·427         | 1·204 | ·846 | ·687 | ·646 |
| All classes ages from 51-70—durations<br>5 and over<br>(Medical and Non-medical) | ·838          | ·833  | ·838 | ·865 | ·824 |
| All classes ages from 71—durations<br>5 and over<br>(Medical and Non-medical)    | ·864          | ·837  | ·868 | ·829 | ·789 |

## APPENDIX V

Comparison of (a) graduated values of  $q_x$  based on data for all classes of assured lives, durations 3 and over, for the two years 1947-48 with (b)  $q_x$  from the A1924-29 ultimate table

| Age<br>$x$ | $q_x$          |                | (a)/(b) | Age<br>$x$ | $q_x$          |                | (a)/(b) |
|------------|----------------|----------------|---------|------------|----------------|----------------|---------|
|            | 1947-48<br>(a) | 1924-29<br>(b) |         |            | 1947-48<br>(a) | 1924-29<br>(b) |         |
| 20         | ·00150         | ·00235         | ·638    | 60         | ·01652         | ·01973         | ·837    |
| 21         | ·00150         | ·00235         | ·638    | 61         | ·01826         | ·02176         | ·839    |
| 22         | ·00150         | ·00235         | ·638    | 62         | ·02019         | ·02394         | ·843    |
| 23         | ·00150         | ·00235         | ·638    | 63         | ·02230         | ·02631         | ·848    |
| 24         | ·00150         | ·00235         | ·638    | 64         | ·02457         | ·02893         | ·849    |
| 25         | ·00150         | ·00235         | ·638    | 65         | ·02699         | ·03188         | ·847    |
| 26         | ·00150         | ·00235         | ·638    | 66         | ·02956         | ·03524         | ·839    |
| 27         | ·00150         | ·00235         | ·638    | 67         | ·03227         | ·03908         | ·826    |
| 28         | ·00150         | ·00236         | ·636    | 68         | ·03512         | ·04338         | ·810    |
| 29         | ·00150         | ·00238         | ·630    | 69         | ·03811         | ·04812         | ·792    |
| 30         | ·00150         | ·00241         | ·622    | 70         | ·04135         | ·05327         | ·776    |
| 31         | ·00151         | ·00246         | ·614    | 71         | ·04496         | ·05881         | ·764    |
| 32         | ·00153         | ·00253         | ·605    | 72         | ·04913         | ·06473         | ·759    |
| 33         | ·00155         | ·00262         | ·592    | 73         | ·05411         | ·07104         | ·762    |
| 34         | ·00159         | ·00273         | ·582    | 74         | ·06012         | ·07777         | ·773    |
| 35         | ·00164         | ·00286         | ·573    | 75         | ·06728         | ·08497         | ·792    |
| 36         | ·00171         | ·00302         | ·566    | 76         | ·07555         | ·09268         | ·815    |
| 37         | ·00180         | ·00320         | ·562    | 77         | ·08469         | ·10093         | ·839    |
| 38         | ·00191         | ·00341         | ·560    | 78         | ·09437         | ·10974         | ·860    |
| 39         | ·00204         | ·00364         | ·560    | 79         | ·10425         | ·11913         | ·875    |
| 40         | ·00220         | ·00388         | ·567    | 80         | ·11414         | ·12910         | ·884    |
| 41         | ·00241         | ·00413         | ·584    | 81         | ·12392         | ·13962         | ·888    |
| 42         | ·00266         | ·00439         | ·606    | 82         | ·13364         | ·15066         | ·887    |
| 43         | ·00296         | ·00466         | ·635    | 83         | ·14367         | ·16221         | ·886    |
| 44         | ·00331         | ·00495         | ·669    | 84         | ·15457         | ·17425         | ·887    |
| 45         | ·00371         | ·00527         | ·704    | 85         | ·16680         | ·18676         | ·893    |
| 46         | ·00414         | ·00563         | ·735    | 86         | ·18051         | ·19973         | ·904    |
| 47         | ·00460         | ·00604         | ·762    | 87         | ·19549         | ·21315         | ·917    |
| 48         | ·00509         | ·00651         | ·782    | 88         | ·21084         | ·22702         | ·929    |
| 49         | ·00561         | ·00704         | ·797    | 89         | ·22501         | ·24134         | ·932    |
| 50         | ·00616         | ·00764         | ·806    | 90         | ·23584         | ·25611         | ·921    |
| 51         | ·00676         | ·00831         | ·813    | 91         | ·24911         | ·27133         | ·918    |
| 52         | ·00743         | ·00906         | ·820    | 92         | ·26606         | ·28700         | ·927    |
| 53         | ·00819         | ·00990         | ·827    | 93         | ·28181         | ·30312         | ·930    |
| 54         | ·00906         | ·01084         | ·836    | 94         | ·29909         | ·31970         | ·936    |
| 55         | ·01003         | ·01190         | ·843    | 95         | ·32005         | ·33675         | ·950    |
| 56         | ·01111         | ·01311         | ·847    | 96         | ·34222         | ·35428         | ·966    |
| 57         | ·01228         | ·01450         | ·847    | 97         | ·36697         | ·37231         | ·986    |
| 58         | ·01355         | ·01608         | ·843    | 98         | ·39977         | ·39086         | 1·023   |
| 59         | ·01496         | ·01783         | ·839    | 99         | ·44518         | ·40995         | 1·086   |
|            |                |                |         | 100        | ·51001         | ·42960         | 1·187   |

## APPENDIX V (cont.)



Graph of the ratio of  $q_x$  from the 1947-48 experience of assured lives, durations 3 and over, to  $q_x$  on the A1924-29 ultimate table

(Note. The 1947-48 values of  $q_x$  have been graduated by the same method as was used in constructing the A1924-29 table.)

## APPENDIX VI

Comparison of 3 % monetary functions based on 1947-48 mortality durations 3 and over, with corresponding values by the A1924-29 ultimate table

## Whole-life functions

| Age<br>$x$ | $a_x$   |          | $A_x$   |          | $P_x$   |          |
|------------|---------|----------|---------|----------|---------|----------|
|            | 1947-48 | A1924-29 | 1947-48 | A1924-29 | 1947-48 | A1924-29 |
| 20         | 25.464  | 24.681   | .22921  | .25199   | .00866  | .00981   |
| 30         | 23.193  | 22.368   | .29535  | .31939   | .01221  | .01367   |
| 40         | 20.136  | 19.307   | .38439  | .40854   | .01819  | .02012   |
| 50         | 16.371  | 15.560   | .49405  | .51767   | .02844  | .03126   |
| 60         | 12.192  | 11.319   | .61581  | .64119   | .04668  | .05205   |
| 70         | 8.084   | 7.241    | .73539  | .75998   | .08095  | .09222   |

## Endowment assurance functions

| Age<br>$x$ | Term<br>$n$ | $a_{x:n-1}$ |           | $A_{x:n}$ |           | $P_{x:n}$ |           |
|------------|-------------|-------------|-----------|-----------|-----------|-----------|-----------|
|            |             | 1947-48     | A 1924-29 | 1947-48   | A 1924-29 | 1947-48   | A 1924-29 |
| $x+n=45$   |             |             |           |           |           |           |           |
| 20         | 25          | 16.646      | 16.472    | .48604    | .49111    | .02754    | .02811    |
| 30         | 15          | 11.163      | 11.071    | .64574    | .64842    | .05309    | .05372    |
| 40         | 5           | 3.695       | 3.679     | .86325    | .86372    | .18387    | .18459    |
| $x+n=50$   |             |             |           |           |           |           |           |
| 20         | 30          | 18.781      | 18.540    | .42384    | .43087    | .02143    | .02205    |
| 30         | 20          | 14.077      | 13.917    | .56088    | .56552    | .03720    | .03791    |
| 40         | 10          | 7.677       | 7.616     | .74727    | .74905    | .08612    | .08694    |
| $x+n=55$   |             |             |           |           |           |           |           |
| 20         | 35          | 20.572      | 20.261    | .37168    | .38075    | .01723    | .01791    |
| 30         | 25          | 16.520      | 16.285    | .48072    | .49655    | .02795    | .02873    |
| 40         | 15          | 11.016      | 10.893    | .65002    | .65360    | .05410    | .05496    |
| 50         | 5           | 3.655       | 3.641     | .86441    | .86483    | .18568    | .18634    |
| $x+n=60$   |             |             |           |           |           |           |           |
| 20         | 40          | 22.047      | 21.666    | .32871    | .33983    | .01426    | .01499    |
| 30         | 30          | 18.532      | 18.219    | .43109    | .44022    | .02207    | .02291    |
| 40         | 20          | 13.766      | 13.567    | .56990    | .57572    | .03860    | .03952    |
| 50         | 10          | 7.490       | 7.430     | .75270    | .75447    | .08866    | .08950    |
| $x+n=65$   |             |             |           |           |           |           |           |
| 20         | 45          | 23.226      | 22.773    | .29437    | .30758    | .01215    | .01294    |
| 30         | 35          | 20.140      | 19.742    | .38424    | .39586    | .01818    | .01909    |
| 40         | 25          | 15.964      | 15.674    | .50588    | .51435    | .02982    | .03085    |
| 50         | 15          | 10.555      | 10.414    | .66755    | .66755    | .05742    | .05849    |
| 60         | 5           | 3.553       | 3.522     | .86740    | .86829    | .19053    | .19201    |
| $x+n=70$   |             |             |           |           |           |           |           |
| 20         | 50          | 24.124      | 23.596    | .26823    | .28361    | .01068    | .01153    |
| 30         | 40          | 21.365      | 20.874    | .34858    | .36289    | .01559    | .01659    |
| 40         | 30          | 17.638      | 17.240    | .45714    | .46874    | .02453    | .02570    |
| 50         | 20          | 12.889      | 12.633    | .59548    | .60292    | .04288    | .04423    |
| 60         | 10          | 7.019       | 6.884     | .76647    | .77037    | .09558    | .09771    |