

### **Proposed Approach for Calculating Capital Relief:**

(Paper: Cairns and El Boukfaoui (2018) to appear in North American Actuarial Journal)

- · Open up communication lines with the regulator
- Establish which method for calculating SCR (and RM)
- Discuss with the regulator
- · Document fully all mortality forecasting models
- Discuss with the regulator
- Run the SCR calculations with and without hedge
- Sensitivity and other robustness tests
- Discuss with the regulator
- Agree capital relief for time 0 and times 1, 2,...



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### **Calculating the SCR Capital Relief**

- L = PV of the full runoff: own liabilities
  - S(t,x) = survivor index for cohort aged x at time 0
- $\tilde{L}$  = PV of the full runoff: synthetic portfolio of liabilities; depends on:
  - $q_G(t, x)$  = general population mortality rates
  - ER(0,t,x) = experience ratios hard coded at time 0
  - $\tilde{S}(t,x)$  = synthetic survivor index
- Experience ratios =>
  - $E[S(t,x)] \approx E[\tilde{S}(t,x)]$
  - $E[L] \approx E[\tilde{L}]$



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#### **Values**

- $L(0) \rightarrow L(1) \rightarrow L(T) \rightarrow L(\infty) = L$
- E.g. L(T) = liability value given mortality experience up to T (point estimate)
- $\tilde{L}(0) \rightarrow \tilde{L}(1) \rightarrow \tilde{L}(T)$
- Hedge payoff  $H(T) = h(\tilde{L}(T))$  $\tilde{L}(T)$ DP
- AP = Attachment Point
- DP = Detachment Point (or Exhaustion Point, EP)



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# "UK" approach

• SCR = 99.5% one-year VaR; based on L(1) - H(1)

Present Value at Time 0	Hedger's liability	Synthetic liability	Hedge payoff
Full runoff	L	$ ilde{m{L}}$	
Valued at Time T	L(T)	$ ilde{m{L}}(m{T})$	H(T)
Valued at Time 1	<i>L</i> (1)	$ ilde{L}(1)$	<b>H</b> (1)
Valued at Time 0	L( <b>0</b> )	$ ilde{L}(0)$	<i>H</i> (0)



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# Original Dutch Approach (incl. Cairns and El Boukfaoui)

• SCR = 99.5% T-year VaR; based on L(T) - H(T)

Present Value at Time 0	Hedger's liability	Synthetic liability	Hedge payoff
Full runoff	L	$ ilde{L}$	
Valued at Time T	L(T)	$\widetilde{L}(T)$	H(T)
Valued at Time 1	<i>L</i> (1)	$\widetilde{L}(1)$	H(1)
Valued at Time 0	L( <b>0</b> )	$ ilde{L}(0)$	H( <b>0</b> )



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#### **Alternative**

- 95% VaR instead of 99.5% (approximately (?) the same as 1-year 99.5% VaR)
  (needs regulator engagement!)
- Full runoff:  $L(\infty) H(T) = L H(T)$  instead of L(T) H(T)

Present Value at Time 0	Hedger's liability	Synthetic liability	Hedge payoff
Full runoff	$L = L(\infty)$	$ ilde{m{L}}$	
Valued at Time T	L(T)	$ ilde{L}(T)$	H(T)
Valued at Time 1	L(1)	$ ilde{L}(1)$	<i>H</i> (1)
Valued at Time 0	L( <b>0</b> )	$ ilde{L}(0)$	H( <b>0</b> )



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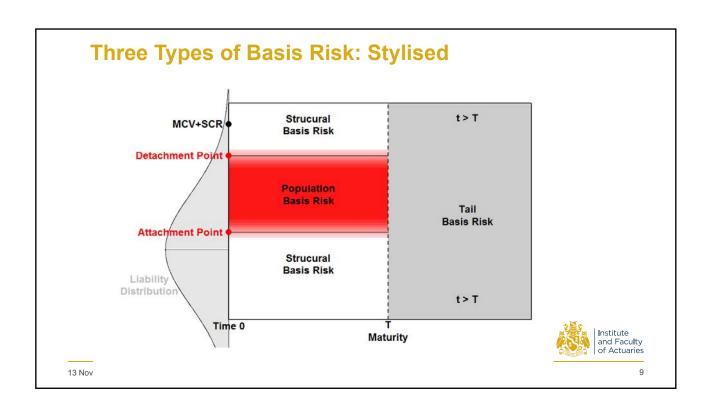
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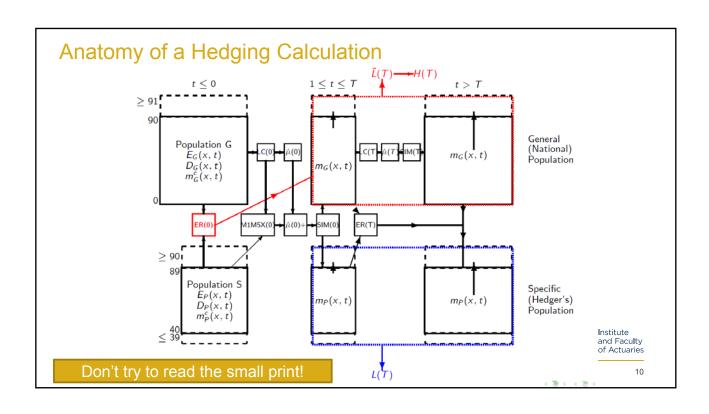
# **Three Types of Basis Risk**

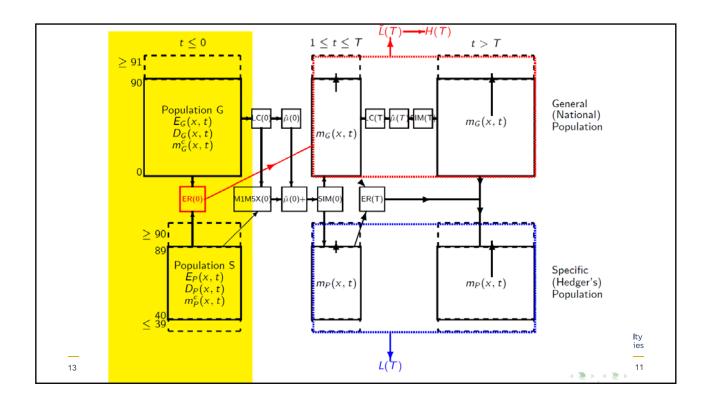
- · Population basis risk
  - Hedger's experience and synthetic index are not perfectly correlated
- Structural basis risk
  - Non-linear payoff => no risk reduction beyond DP or below AP
- Tail basis risk
  - Cashflows after maturity, T:
    - ullet Depend on risk emerging before T and after T
    - Risks before T are (can be) hedged
    - Additional risks emerging after maturity, T, are not hedged

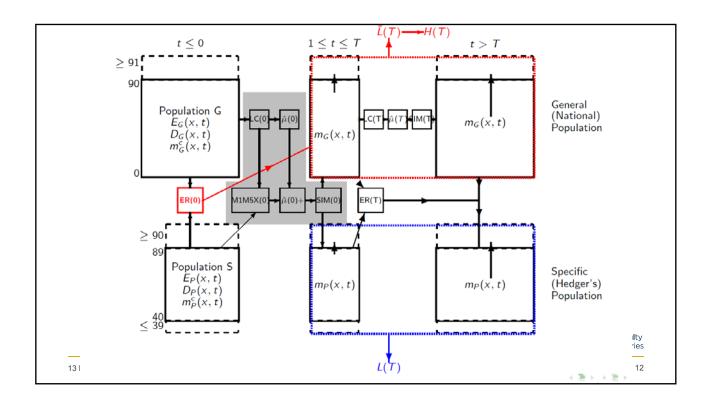


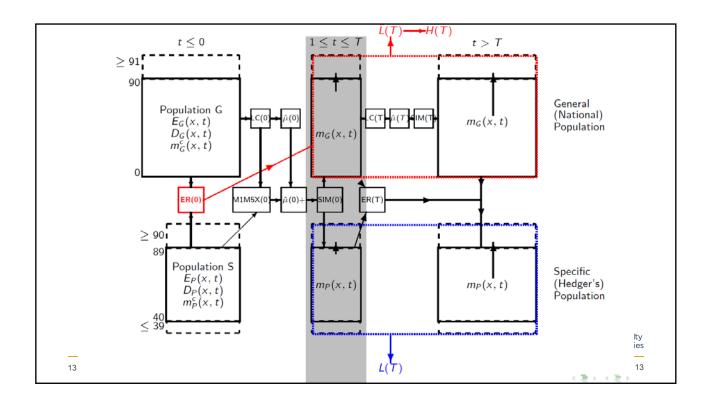
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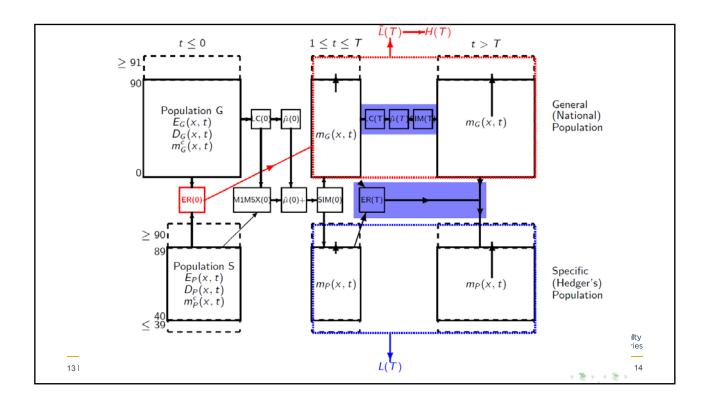


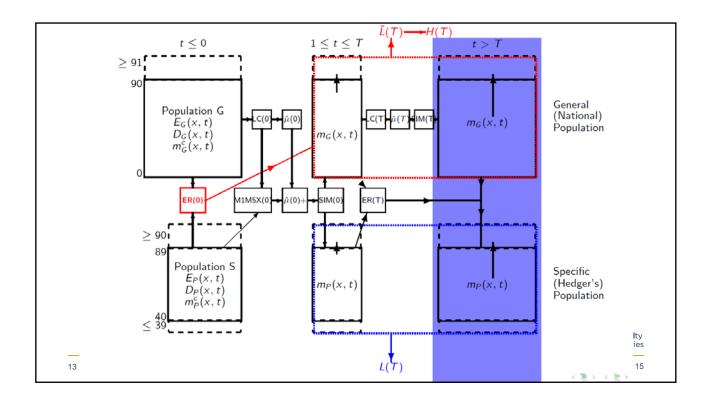


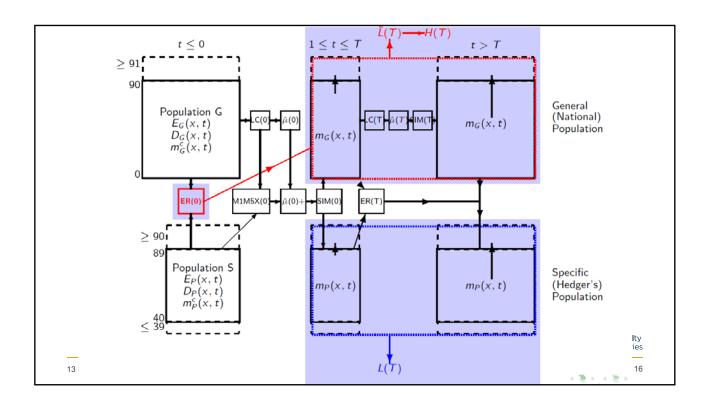












### **Capital Relief Calculation Summary**

- Simulated L(T), H(T) => hedged distribution => capital relief
- In advance, discuss and agree with the regulator the following:
  - Break down the process into a series of manageable steps
  - Document all of these steps carefully
  - Document clearly all of the models being used in each step



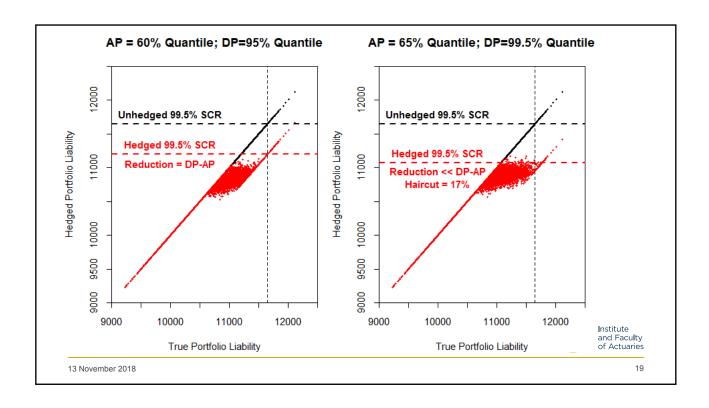
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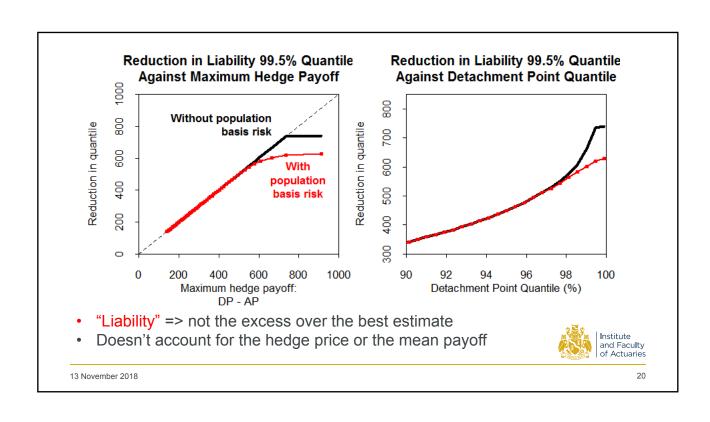
## Simulated Impact of Hedge at Time T

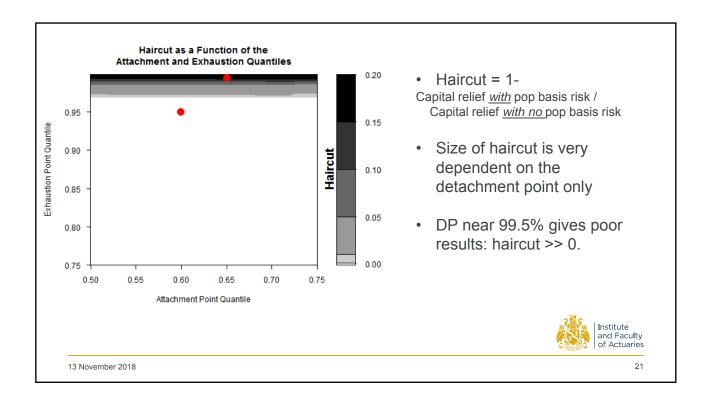
- Dutch insured lives dataset versus Dutch national mortality data
- Portfolio = mixture of deferred and immediate annuities
- · Hedge: 10-year bull spread
- Case 1
  - AP=60% quantile of the synthetic liability
  - DP=95% quantile
- Case 2
  - AP=65% quantile
  - DP=99.5% quantile



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## **Further reading**

- · Paper:
  - Cairns, A.J.G., and El Boukfaoui, G. (2017)
    Basis Risk in Index Based Longevity Hedges: A Guide For Longevity Hedgers
    To appear in North American Actuarial Journal
  - Available at:
    - www.macs.hw.ac.uk/~andrewc/ARCresources
    - www.actuaries.org.uk/ARC



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