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Traditional method of projecting populations $\qquad$
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- Project age-sex mortality rates
- Breakdown current population by age-sex
- The projected population for the following year is the current population plus assumed net immigration for the period plus $\qquad$ births less deaths determined by mortality rates
- Continue projection for required number of years $\qquad$
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Key demographic questions $\qquad$
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- How do populations age and grow?
- Is there any upper limit to age?
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- Are there other methods we can use to project populations?
- Are these methods more accurate? $\qquad$
- What size of difference will it make?
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## Aspects discussed

- Simple conceptual model which can be tested against data
- Empirical results from England and Wales
- Evidence that survival approach gives more accurate results than mortality based approach
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Empirical results $\qquad$

- Applied to England and Wales from 1800 to 2003
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- Looked for evidence of which model worked best in different time periods $\qquad$
- Looked for evidence of maximum age
- Used results to project UK population and compare accuracy $\qquad$
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## Towards a maximum age?


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Convergent case based on females from England and Wales, 1901 to 1946 with fitted regression lines

Convergence results $\qquad$

| Converging percentiles | Age of death where convergence occurs | Required expected future lifetime at age 1 | Calendar Year this occurs |
| :---: | :---: | :---: | :---: |
| $10^{\text {ma }}$ and $20^{\text {mm }}$ | 83.91 | 83.16 | 1988 |
| $20^{\text {th }}$ and $30^{\text {mm }}$ | 84.06 | 83.24 | 1989 |
| $30^{\text {ma }}$ and $40^{\text {mm }}$ | 86.14 | 84.96 | 1994 |
| $40^{\text {at }}$ and $50^{\text {am }}$ | 88.47 | 87.46 | 2003 |
| $50^{\mathrm{mm}}$ and $60^{\mathrm{mm}}$ | 92.28 | 92.58 | 2019 |
| $60^{\text {ma }}$ and $70^{\text {am }}$ | 98.82 | 103.19 | 2055 |
| $70^{\text {a }}$ and $80^{\text {(1) }}$ | 102.89 | 110.86 | 2080 |
| $80^{\mathrm{m}}$ and $90^{\text {m }}$ | 106.05 | 117.8 | 2103 |

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But convergence pattern ceases after 1946 and so no maximum
$\qquad$ age is any longer indicated in the data so must look for reasons
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## Life expectancy at age 80


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## Population forecasting based on survival

Procedure:

1. Establish relationship between the percentiles and the expectation of life at a given age (we use age 50)
2. Establish nature of linear relationship between calendar year and expectation of life
3. Project forward expectation of life using the relationship found in stage 2
4. Derive survival percentiles using the projected expectation of life and the relationship derived in stage 1
5. Derive mortality from resultant life tables and proceed as normal

## Gompertz Makeham equation

- A problem with using the full life table is the volume of data required.
- A more suitable solution can thus be to determine a function that fits the data so that only a few parameters are required.
- The function chosen to fit the data is a form of the GompertzMakeham Model which gives a very good fit to the data
- The Gompertz-Makeham Model provides a function for the force of mortality and is defined as:
$\mu_{x}=A+B c^{x}$ or $\mu_{x}=A+B e^{\gamma x_{x}}$ where $\gamma=\ln (c)$
- Where $x=$ age and $A, B$ and $c$ are parameters $\qquad$
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Validity testing using retro-projections based on 1981
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- To show suitability of the projections we compare projections from our model, with the GAD projection and actual survival from a 1981 base
- GAD's published projection was obtained by constructing life tables using the projected mortality rates at the time
- We use a survival approach but otherwise the same starting data as GAD's
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Predicted survival curves at age 50 for year 2000

## using 1981 base

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Comparison of projected life tables for 2000 for England and Wales males

Comparison of percentage error between actual, GAD and model 1982 to 2003

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A comparison of 50+ population projections to 2020 based on GAD and on model ~ trend in male life expectancy at age 50
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year
We used ARIMA techniques to check that projected life expectancy were within the $95 \%$ confidence interval
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A comparison of $50+$ population projections to 2020 based on GAD and on model ~ base 2001
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| age | GAD 2020 | Model | Diff | Diff $\%$ |
| :--- | ---: | :---: | :---: | ---: |
| $50-59$ | $3,788,205$ | $3,809,512$ | 21,306 | $0.56 \%$ |
| $60-69$ | $3,014,841$ | $3,111,925$ | 97,084 | $3.22 \%$ |
| $70-79$ | $2,324,314$ | $2,504,966$ | 180,653 | $7.77 \%$ |
| $80-89$ | 978,574 | $1,164,099$ | 185,525 | $18.96 \%$ |
| total | $10,105,934$ | $10,590,502$ | 484,568 | $4.79 \%$ |

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Difference for females was 110,858 on same basis, so total difference is nearly 0.6 m people between GAD and model (equates to additional state pension costs of $£ 3$ bn per annum)

## Conclusions

- We have offered a new way of charting the development of populations through an analysis of trends in human survival based on ordinary life tables
- We sought to explain the various different shapes of survival curves starting with a simple model. This conjectured three basic patterns of survival: (a) 'divergent', (b) 'convergent' or (c) 'parallel'
- There is currently no convergence towards a maximum age $\qquad$ although this was not true before 1946. Extended survival patterns among the oldest old is one of the reasons $\qquad$
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## Conclusions

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- Population projections based on survival trends rather than mortality trends produced more accurate projections of the England an Wales populations than GAD projections to 2003 from a 1981 base
- Population projections to 2020 using our model show 0.6 m more people aged 50+ than GAD projections
- There is scope to develop the model in a range of applications and across countries $\qquad$
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