

The Actuarial Profession  
making financial sense of the future

Estimating and Communicating Reserving  
Uncertainty  
4<sup>th</sup> Younger Members Convention

James Toller  
Christian Kortebein

The City Hall, Cardiff, 5-6 December 2005

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Agenda

- Section 1: Working party findings
- Section 2: Models in Allianz
- Section 3: Beazley – useful models?

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Section 1: What did we learn?

- “Reasonable” actuaries come up with variable results - wider than would be expected even allowing for blind reserving conditions
- Wide range of results from different methods/models
- Range still wide even when same method/model used
- No “correct” method/model apparent

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## Approach vs. needs



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## Why measure reserve uncertainty?

Increasingly, we are being asked to quantify:

- a range of reasonable best estimates
- a range of reasonable outcomes around the actuarial best estimate
- what confidence level the held reserve is compared to the actuarial best estimate
- how likely future payments will be X% higher than the held reserve

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## Why measure reserve uncertainty?

In part, these questions are the result of new regulations and accounting rules, such as:

- ICA
- Solvency II
- IFRS
- Sarbanes Oxley, Morris, etc.

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## Reserving uncertainty

### Reserving is about forecasting unpaid claims:

- The variability of a forecast includes the estimation variance and the process variance:

$$\text{prediction error} = (\text{process variance} + \text{estimation variance})^{1/2}$$

- However, what we are really interested in is a predictive distribution of outstanding claims (ultimate claims and the associated cash flows)

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## A simple example

- Data sample  $Y = \{3, 8, 5, 9, 5, 8, 4, 8, 7, 3\}$
- Expected value = 6
- What is the best estimate of a new forecast value?
- What is the prediction error of a new forecast value?
- What is the predictive distribution of a new forecast value?

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## Analytic Solution

- Random variable is Poisson distributed

$$\text{standard error} = \frac{\sigma}{\sqrt{n}}$$

$$\text{process variance} = \mu$$

$$\text{prediction error of forecast} = \left(\mu + \frac{\sigma^2}{n}\right)^{1/2}$$

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## Parameter Uncertainty (Bootstrapping)

- Simple method to obtain a distribution of parameters
- Many new data sets are created by sampling with replacement from the observed data
- Result is a “simulated” distribution of parameters

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## Parameter Uncertainty (Bootstrapping)

Observed Data											Mean
	3	8	5	9	5	8	4	8	7	3	6

Bootstrap Samples											Mean
1	8	5	3	7	9	3	3	5	9	7	5.9
2	3	3	9	5	8	8	8	3	5	5	5.7
3	8	3	8	7	9	4	9	5	7	8	6.8
4	4	5	5	3	8	9	3	3	7	3	5.0
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10,000	4	9	8	3	5	8	4	4	8	8	6.1

Bootstrap standard error 0.68

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## Predictive Distribution

Assuming Poisson process

Observed Data											Mean
	3	8	5	9	5	8	4	8	7	3	6

Bootstrap Samples											Mean
1	8	5	3	7	9	3	3	5	9	7	5.9
2	3	3	9	5	8	8	8	3	5	5	5.7
3	8	3	8	7	9	4	9	5	7	8	6.8
4	4	5	5	3	8	9	3	3	7	3	5.0
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10,000	4	9	8	3	5	8	4	4	8	8	6.1

Bootstrap standard error 0.68

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Simulated Forecast
7
4
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2.54 Prediction error

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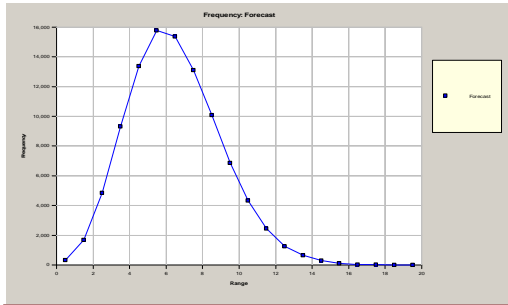
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## Predictive Distribution



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## Stochastic Reserving and Bootstrapping

- Define and fit statistical model
  - Overdispersed Poisson Model
  - Mack
  - or any other model than can be clearly defined
- Obtain residuals and pseudo data
- Refit statistical model to pseudo data
- Obtain forecast

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## Bootstrapping the Chain Ladder (ODP)

- Fit chain ladder model
- Obtain Pearson residuals  $r_p = \frac{C - \mu}{\sqrt{\mu}}$
- Resample residuals
- Obtain pseudo data  $C' = r_p \sqrt{\mu} + \mu$
- Use chain ladder to re-fit model, and estimate future incremental payments

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## Bootstrapping the Chain Ladder (ODP)

- Simulate observation from process distribution assuming mean is incremental value obtained at Step 5
- Repeat many times, storing the reserve estimates
- Prediction error is then standard deviation of results

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## What is being modelled?

- For a given model and for a given data set:
  - uncertainty in a forecast around an assumed development pattern due to observed historic variability taking account of
    - parameter risk
    - process risk
  - assuming
    - development pattern is the same for all origin periods
    - origin periods are independent

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## What is not being modelled?

- Model risk
  - if the underlying model is wrong, the results will be wrong
- Risks that do not appear in the data
- Other risks
  - some operational risks
  - regulatory risk
  - future changes in legislation
  - etc.

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### Use of Models at Allianz

- Additional Management Information
- Preparation for Solvency II and IFRS Phase II
- Internal Risk Capital Assessment (not yet fully implemented)
- Additional Insight into Traditional Reserving Process

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### Section 3: Beazley – useful models?

#### Beazley's objectives

- Business planning – Efficient capital use
  - Capital cost over lifetime of policy
  - Risk adjusted returns on capital
- Reserve setting – Prudential risk margins
  - Is the level of prudence in our reserves changing?

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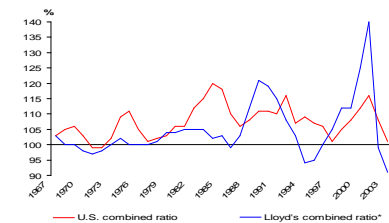
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### Section 3: Beazley Background

#### Market cycles

- Are London Market swings more severe?



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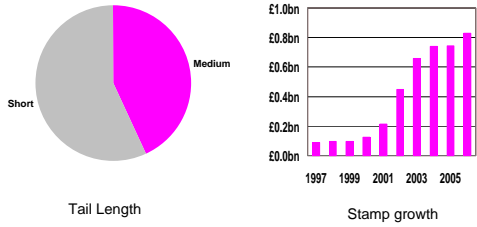
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### Section 3: Beazley Background



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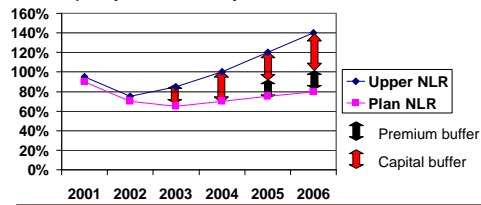
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### Section 3: Review objectives

We need to produce the following chart

- By class and team for interest
- Company level is key



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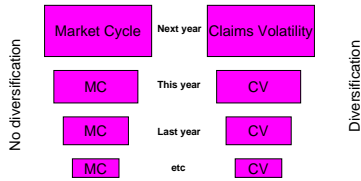
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### Section 3: Beazley approach



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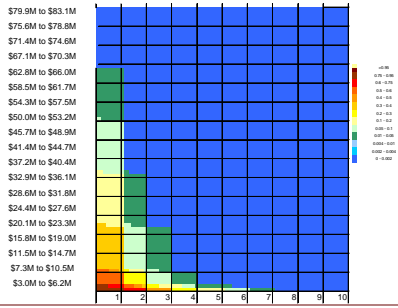
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### Section 3: Claims volatility



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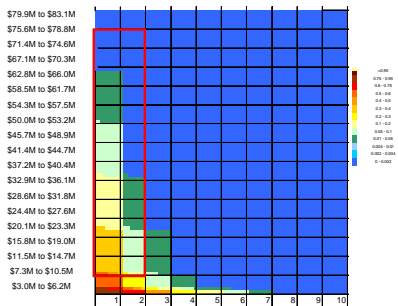
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### Section 3: Claims volatility



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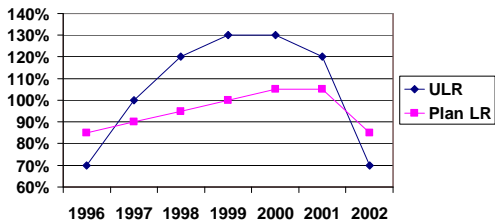
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### Section 3: Market cycle



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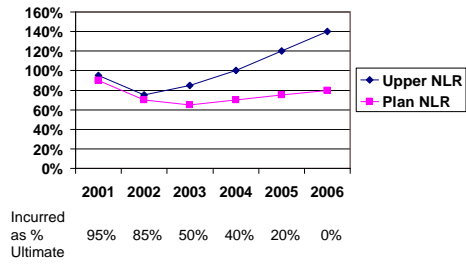
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### Section 3: Risk reduction



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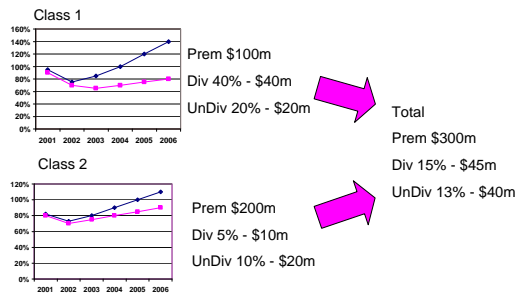
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### Section 3: Combination (e.g. 2006)



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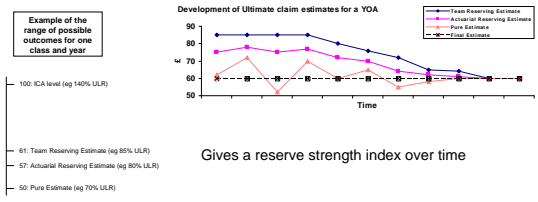
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### Section 3: Uses - Reserve strength



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Questions?

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**Task Force on Pedagogical**  
Making Pedagogical Research Visible

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